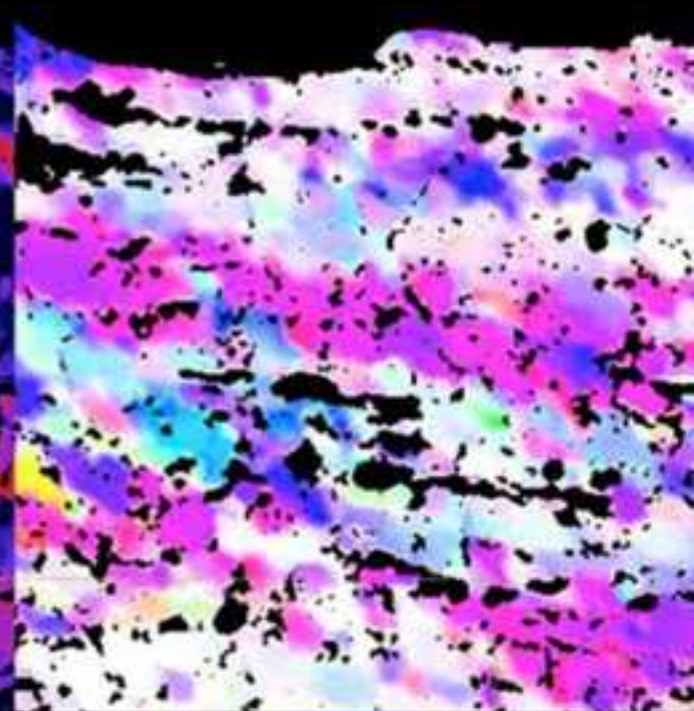
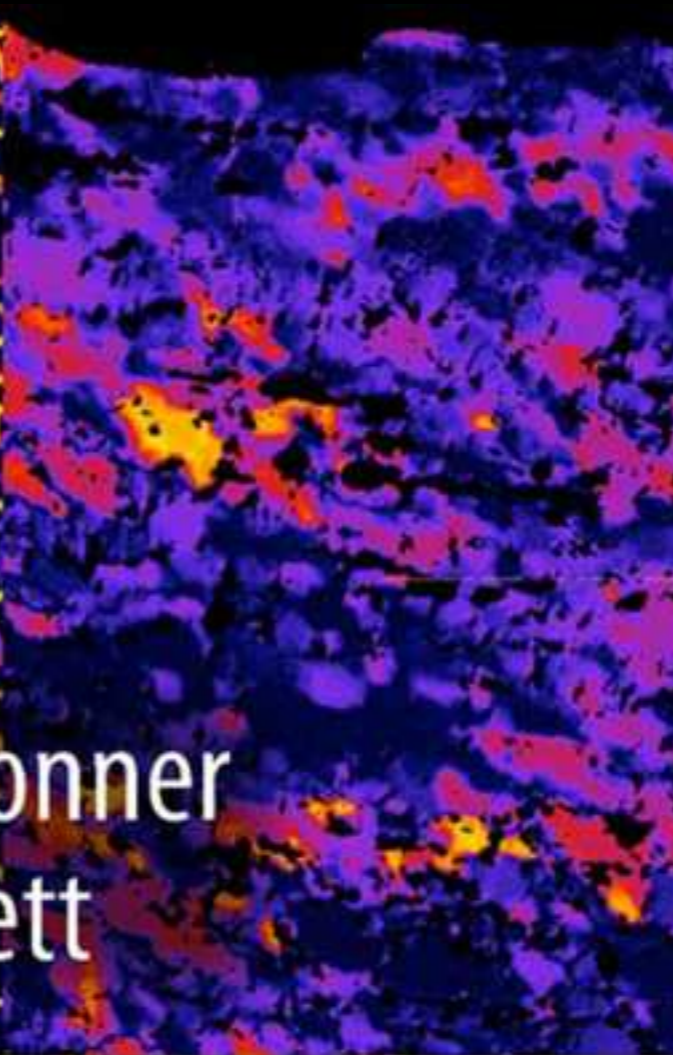
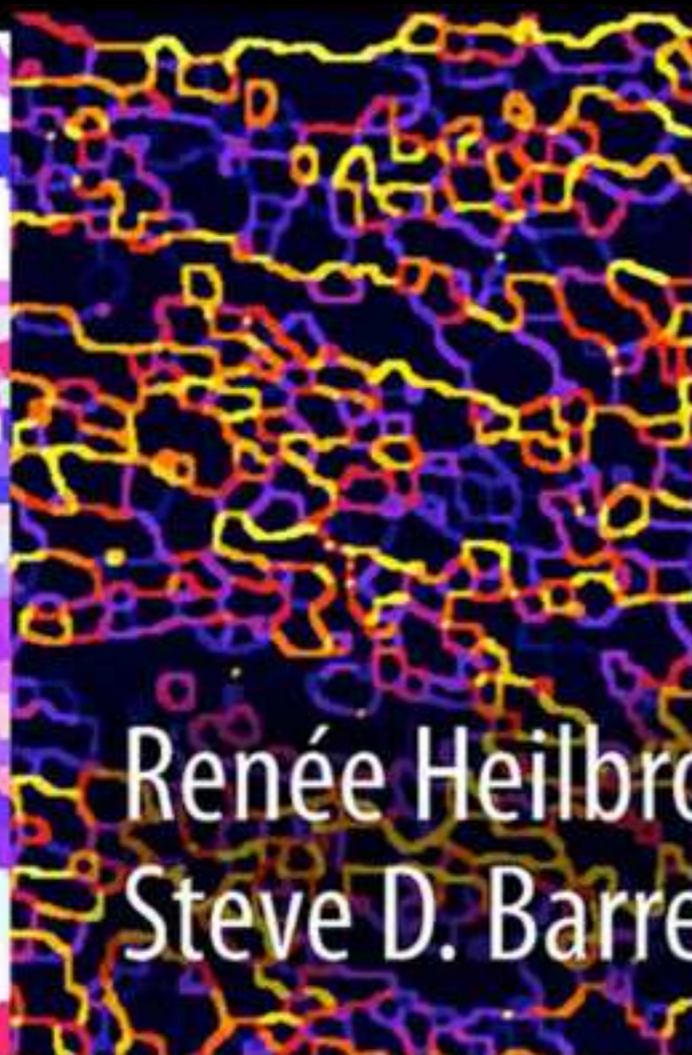


DRT 2015 Aachen, September 9-11, 2015



Renée Heilbronner  
Steve D. Barrett



# Image Analysis in Earth Sciences

# 25 minutes stroll through the book...

... by way of two examples

1. Black Hills Quartzite revisited  
with Jan Tullis

2. Work in progress:

The microstructure of 70:30 olivine-orthopyroxene mixtures  
experimentally deformed at 1200°C  
with Miki Tasaka

and a take-home message

and an announcement

and ... somebody has to turn off the microphone

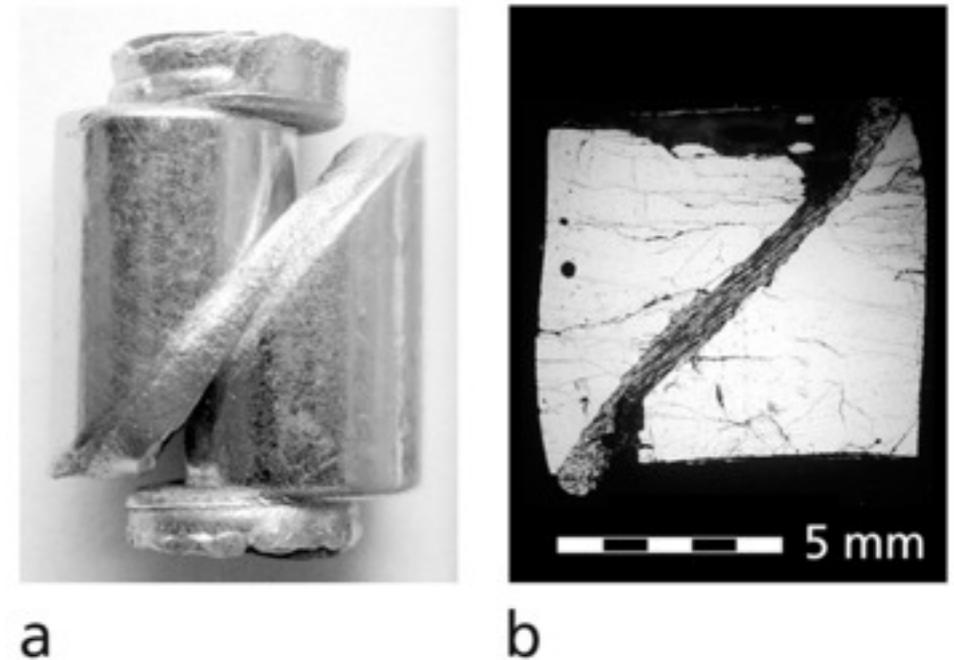
# the publication

JOURNAL OF GEOPHYSICAL RESEARCH, VOL. 111, B10202, doi:10.1029/2005JB004194, 2006



## Evolution of c axis pole figures and grain size during dynamic recrystallization: Results from experimentally sheared quartzite

Renée Heilbronner<sup>1</sup> and Jan Tullis<sup>2</sup>



**Figure 1.** Geometry of experimentally sheared Black Hills quartzite samples. (a) Jacketed sample after general shear deformation: BHQ sheared between  $45^\circ$  pre-cut Brazil quartz pistons (total undeformed length  $\approx 15$  mm, diameter = 6.3 mm), which are able to slide horizontally relative to the upper and lower  $ZrO_2$  pistons. (b) Thin section of sheared BHQ sample and Brazil quartz pistons under circularly polarized light. Horizontal cracks in the pistons result from unloading.

# results

## experimental conditions:

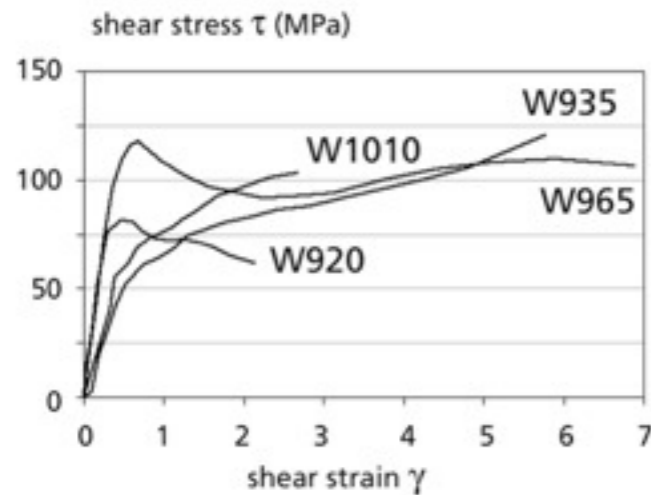
$$T = 915^{\circ}\text{C}$$

$$p_c = 1.5 \text{ GPa}$$

$$\dot{\gamma} = 2 \cdot 10^{-5} \text{ s}^{-1}$$

(~ regime 3)

## shear stresses:



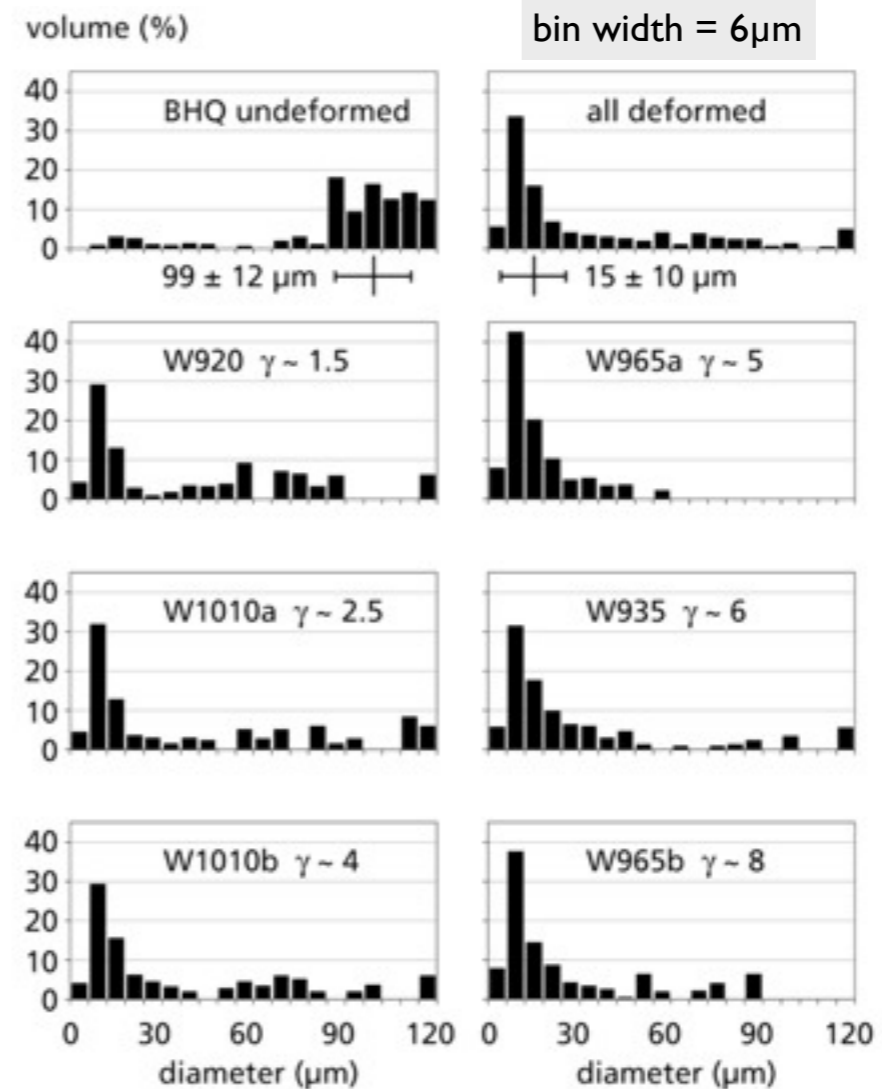
$$\tau \approx 100 \text{ MPa}$$

$$\Delta\sigma \approx 200 \text{ MPa}$$

**Figure 2.** Shear stress–shear strain curves for the four samples used in this study; for deformation conditions and percent thinning see Table 1.

(Heilbronner & Tullis, JGR, 2006)

## 3D grain size:



mode of  
recrystallized  
grain size (3D):  
 $D \approx 12 \mu\text{m}$

**Figure 5.** Grain size distribution of undeformed Black Hills quartzite (BHQ) and three experimentally sheared samples. Volume percent of 3-D grains as a function of the diameter of a sphere of the same size. Undeformed BHQ, summary of all deformed samples; W920 ( $\gamma \approx 1.5$ ); W1010a ( $\gamma \approx 2.5$ ); W1010b ( $\gamma \approx 4$ ); W965a ( $\gamma \approx 5$ ); W935 ( $\gamma \approx 6$ ); and W965b ( $\gamma \approx 8$ ). Average grain diameters of undeformed BHQ and recrystallized grains have been determined for grain sizes  $>60$  and  $<48 \mu\text{m}$ , respectively.

# why go back ?

motivation:

re-measure CIP grain size using EBSD

analyze Betti's quartz - coesite experiments @ high resolution

verify Stipp & Tullis piezometer

step 1: CIP vs EBSD grain size - rewrite STRIPSTAR

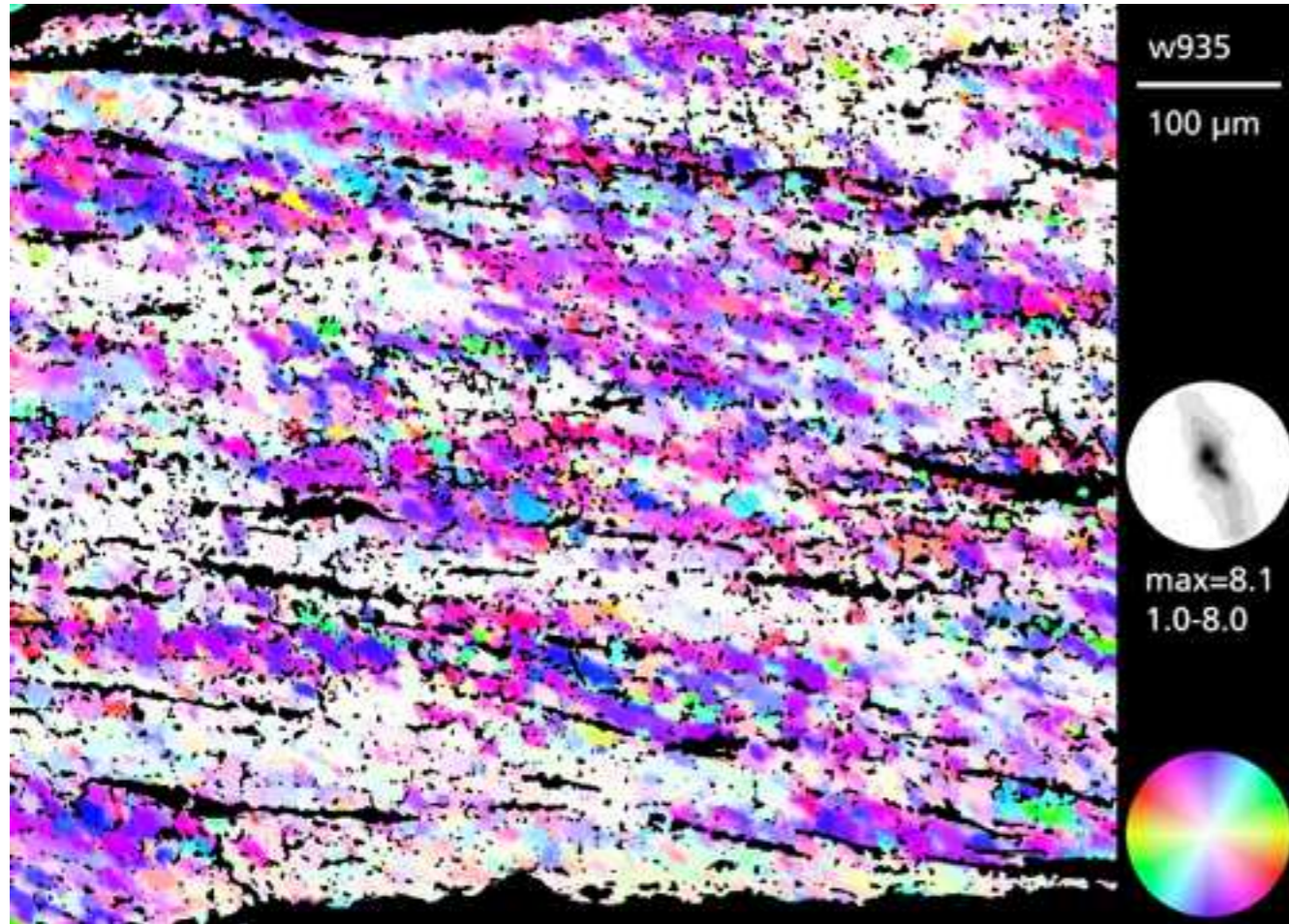
step 2: decide on "the mean grain size"

step 3: test piezometer

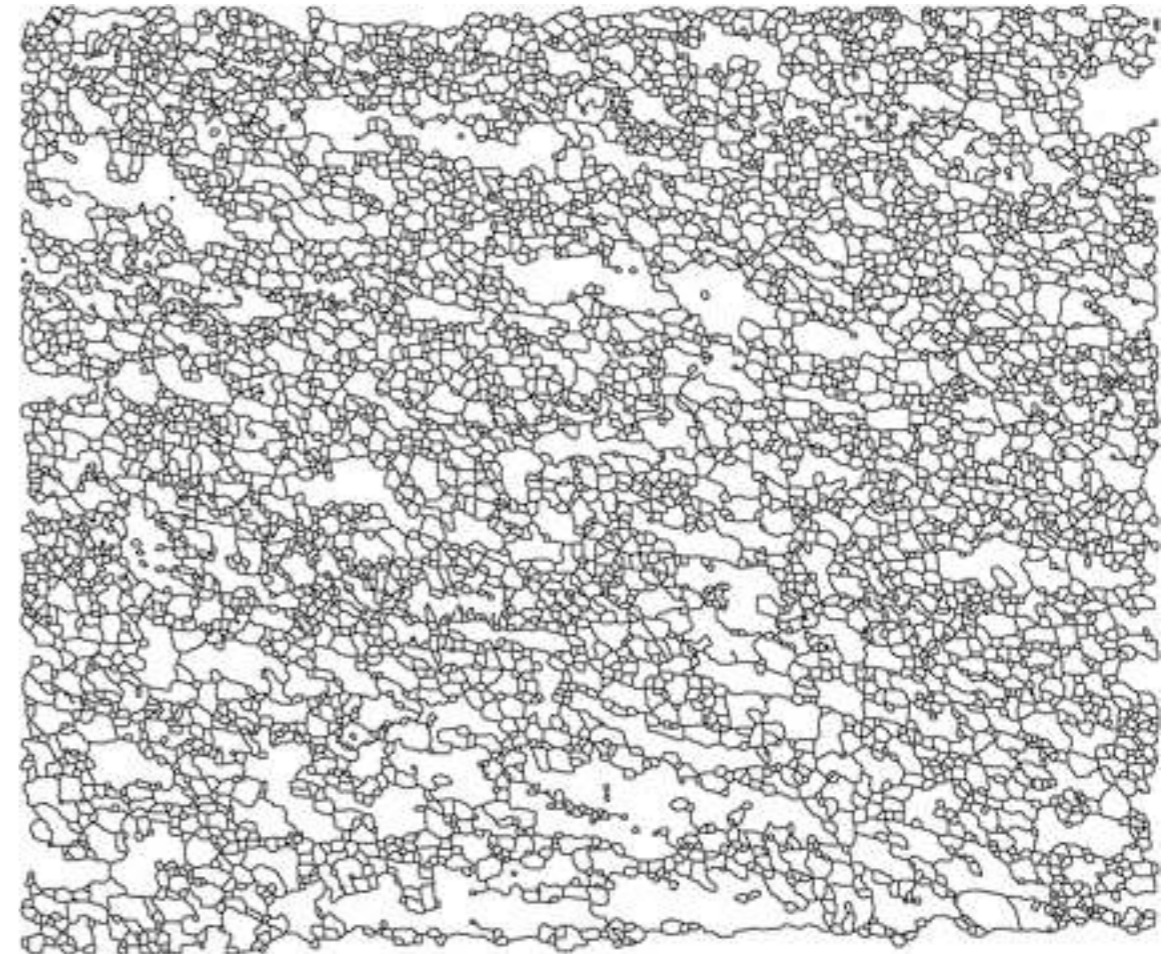
step 4: .... see Betti's poster and PhD

⇒ *reculer pour mieux sauter*

# light microscopy - CIP



w935 c-axis orientation image (COI)

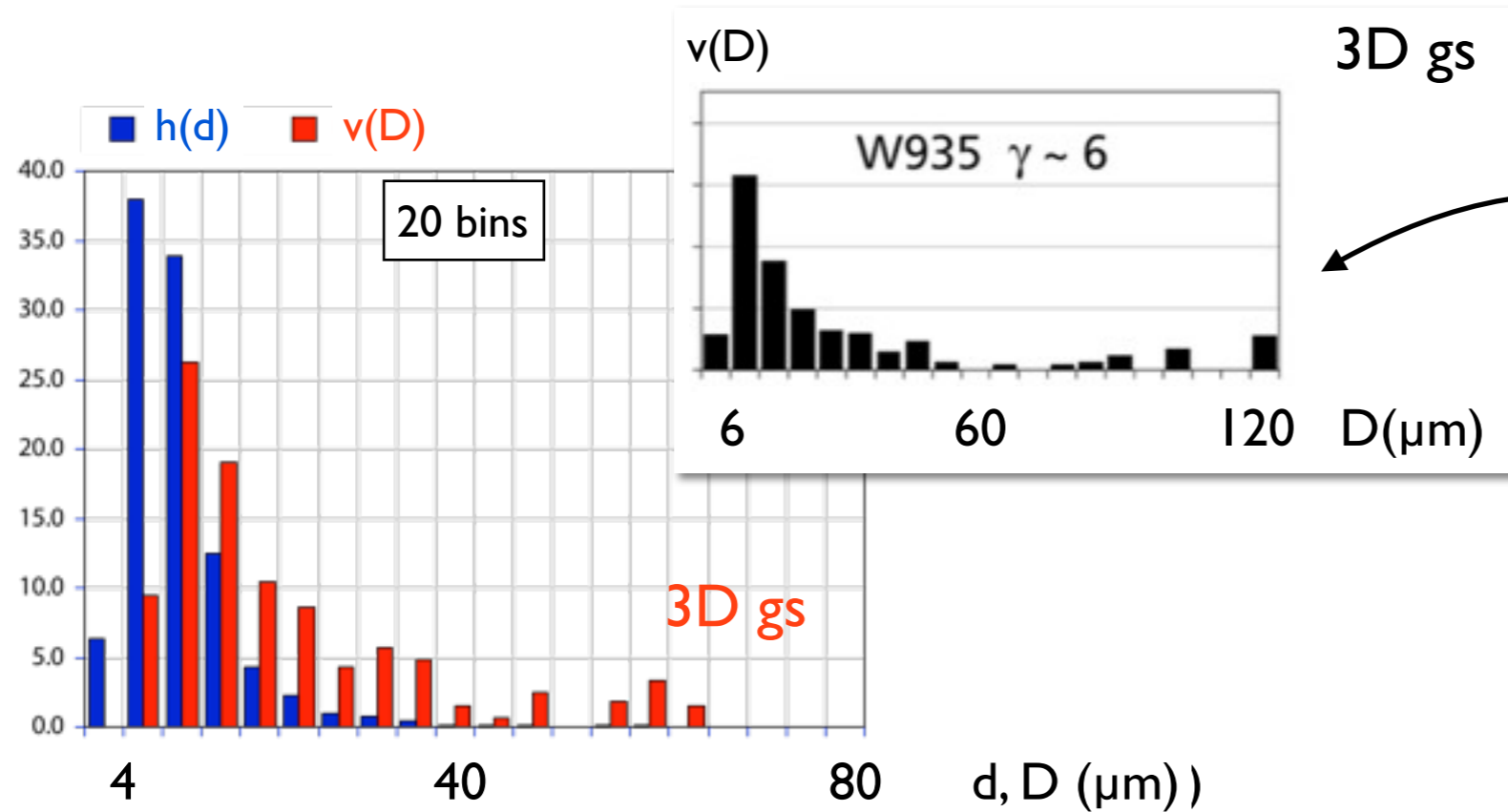


w 935 grain boundary map

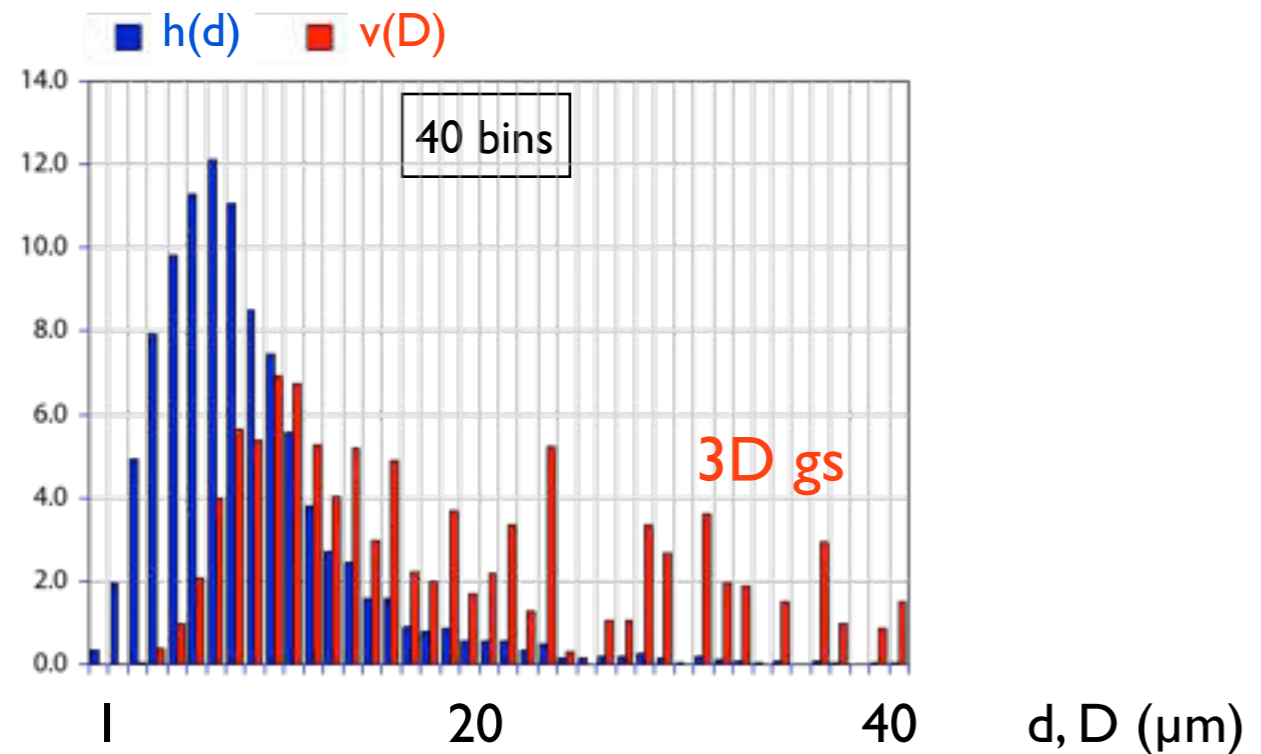
for segmentation, see many chapters in:  
Heilbronner & Barrett, Springer (2014)

⇒ *segmentation is a pain*

# CIP grain size at higher resolution



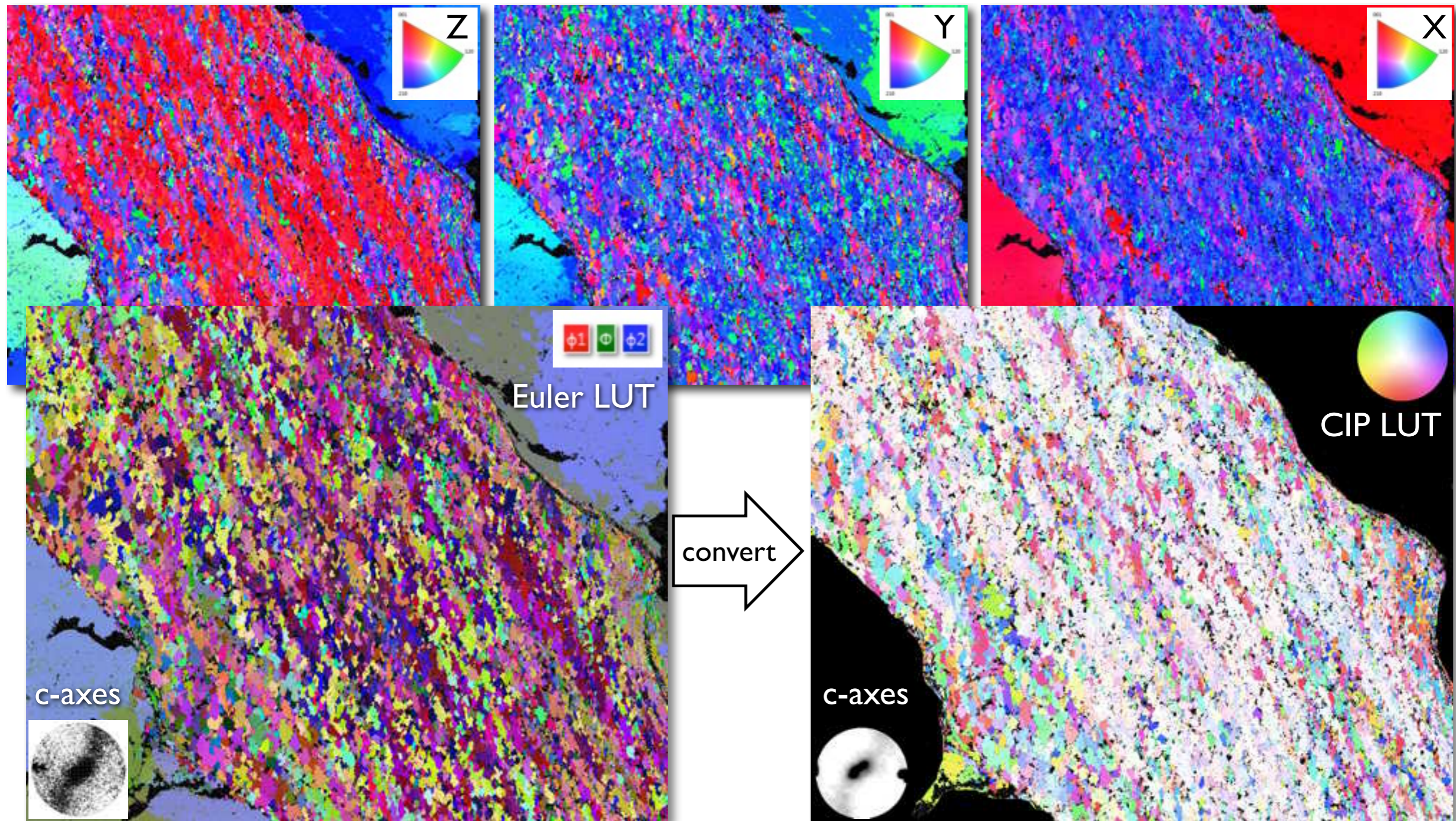
	d( $\mu\text{m}$ )	D( $\mu\text{m}^3$ )
Mode		bin(6-12)
Mode	bin(4-8)	bin(8-12)



	d( $\mu\text{m}$ )	D( $\mu\text{m}^3$ )
Mean	9.7	
RMS	11.4	
Mode	bin(6-7)	bin(9-10)

$\Rightarrow$  new STRIPSTAR = improvement

# EBSD map of same sample



(Heilbronner & Barrett, Springer, 2014)

$\Rightarrow$  use *c-axis* orientation for visualization



# grain maps CIP and EBSD

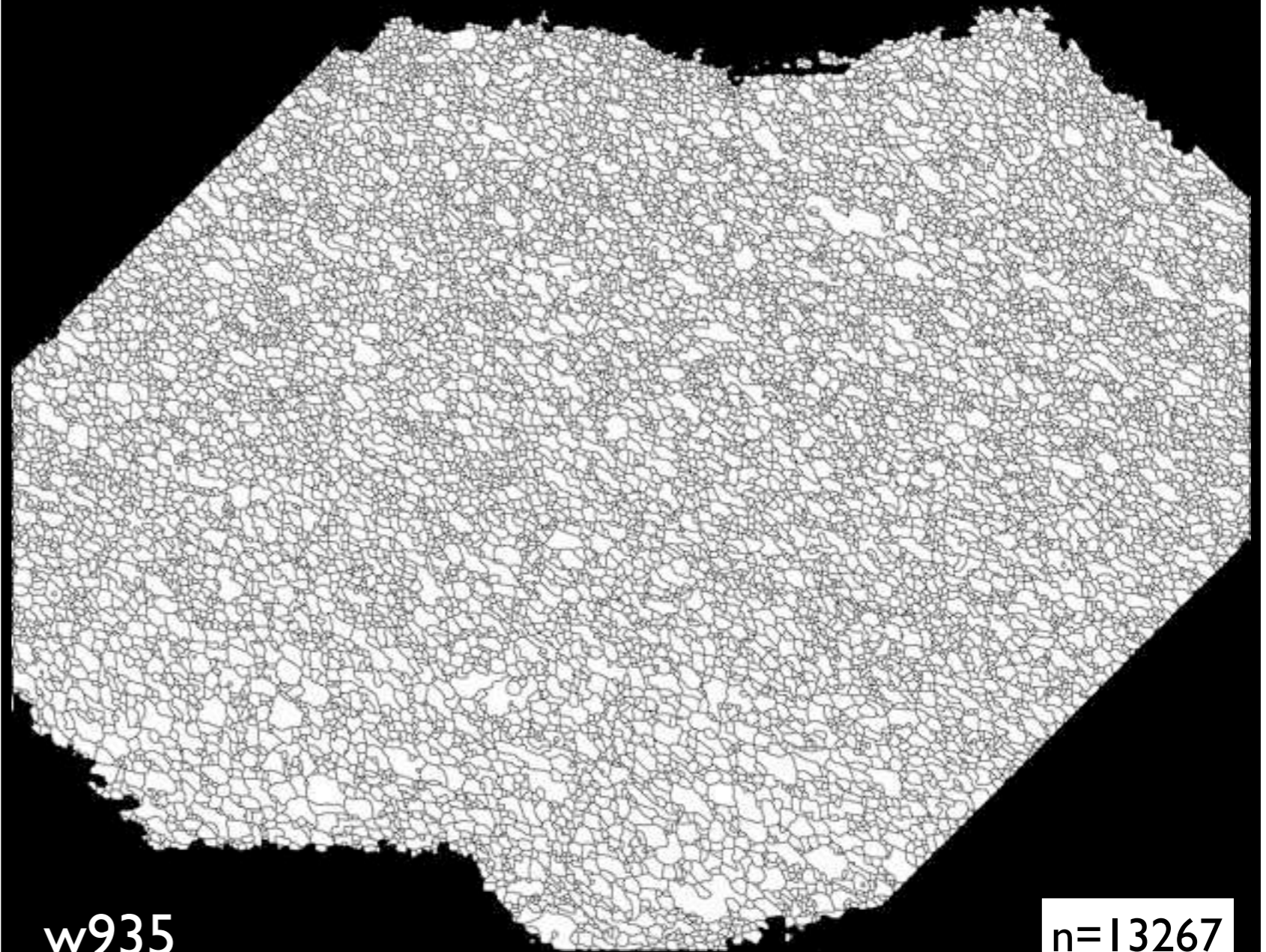
CIP grain map



w935

n=3605

EBSD grain map

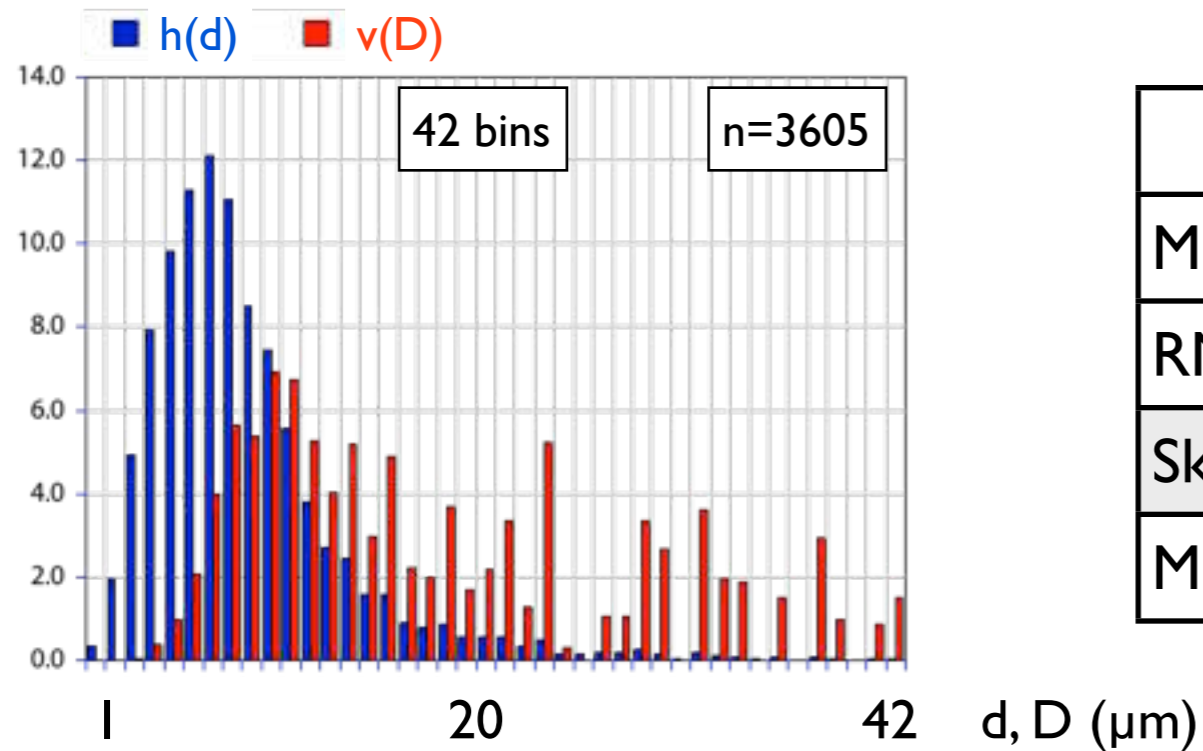


w935

n=13267

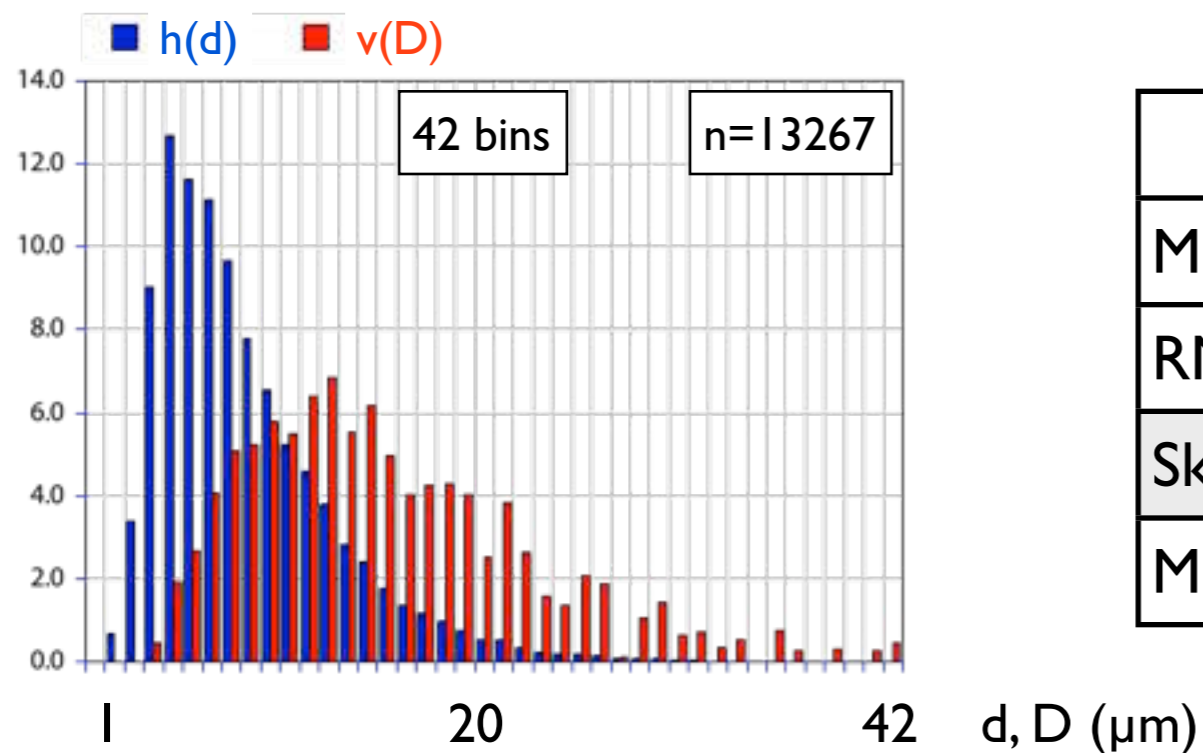
⇒ *segmentation is easy*

# grain size from LM and SEM



## CIP

	d(μm)	D(μm)	D(μm <sup>3</sup> )
Mean	9.721	8.075	17.907
RMS	11.353		
Skewness	2.013	2.385	0.727
Mode	bin(6-7)		bin(9-10)



## EBSD

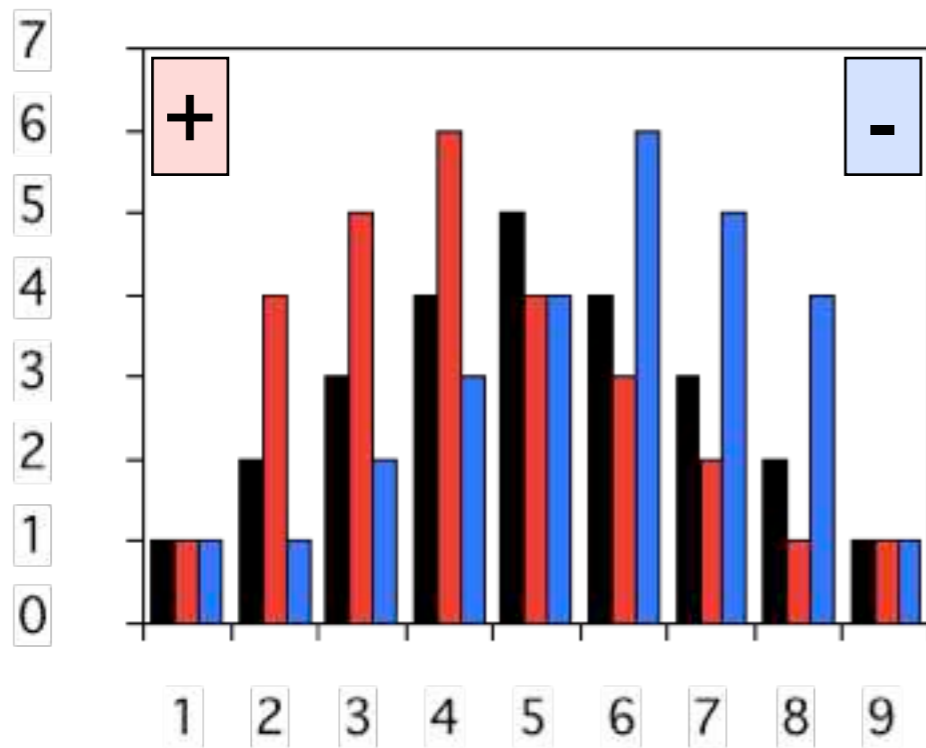
	d(μm)	D(μm)	D(μm <sup>3</sup> )
Mean	8.291	7.915	15.357
RMS	9.502		
Skewness	1.509	1.774	0.930
Mode	bin(4-5)		bin(12-13)

⇒ *CIP grain size = EBSD grain size*

# finding the right mean...

arithmetic mean	$\bar{X}$	=	$1/n \cdot \sum x_i$
geometric mean	$G$	=	$\sqrt[n]{\prod x_i}$
harmonic mean	$H$	=	$1 / (1/n \cdot \sum 1/x_i) = n / \sum 1/x_i$
root-mean-square	RMS	=	$\sqrt{(1/n \cdot \sum x_i^2)} \approx$ area average
Median	=	$\begin{cases} x_{(n+1)/2} & \text{if } n = \text{odd} \\ (x_{n/2} + x_{n/2+1}) / 2 & \text{if } n = \text{even} \end{cases}$	
Mode	=	most frequent value	

$$RMS > \bar{X} \geq G \geq H$$

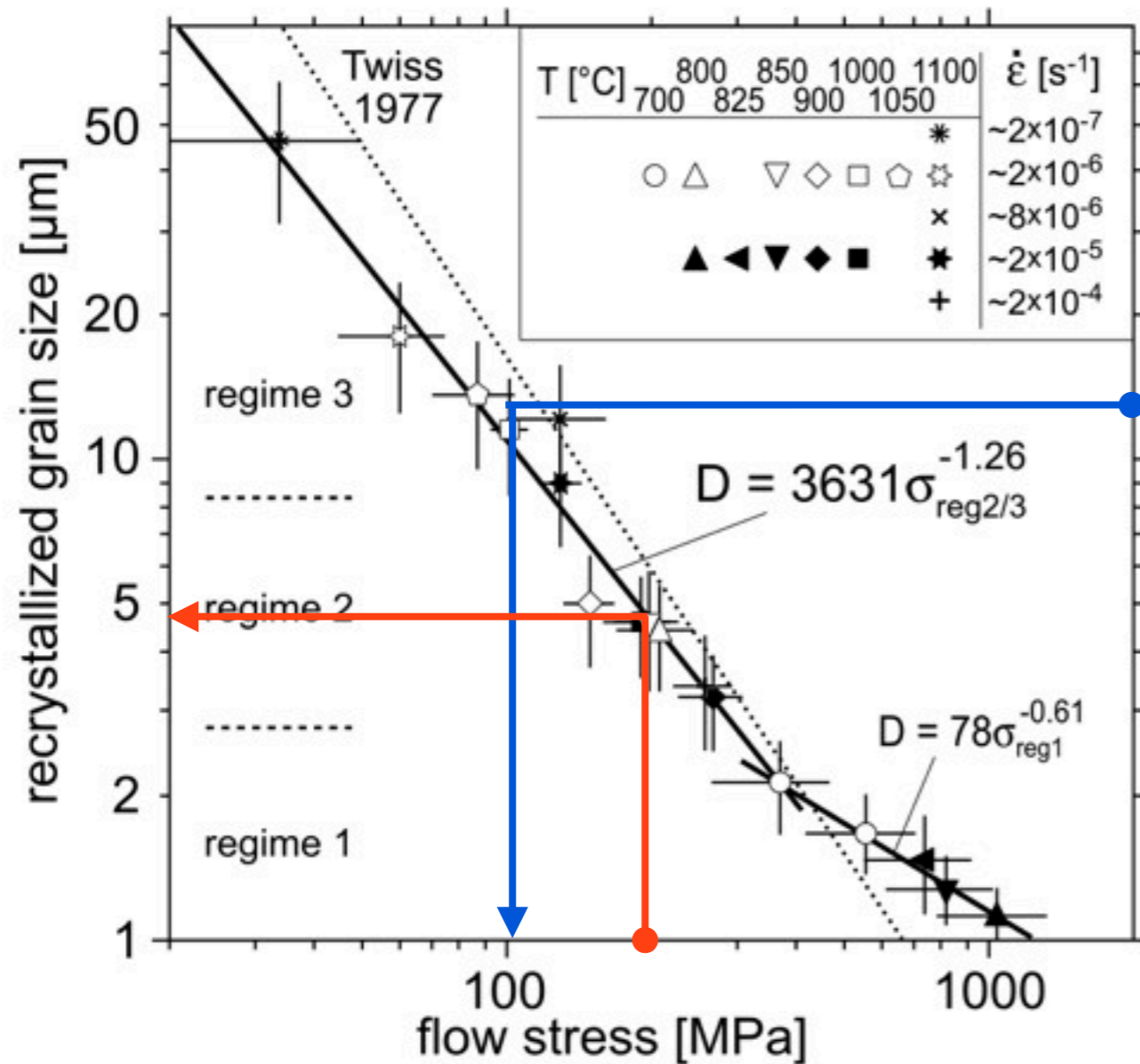


$\bar{X}$   
 Mode  
 RMS  
 Skewness  
 RMS/ $\bar{X}$

symm.	+ skew	- skew
5.00	4.33	5.67
5.00	4.00	6.00
5.39	4.75	5.99
0.00	0.53	-0.53
<b>108%</b>	<b>110%</b>	<b>106%</b>

$\Rightarrow$  *RMS overestimates mean*

# check the piezometer



$$\text{RMS}(d) = 10 (3.56 \pm 0.27) \cdot \sigma^{-(1.26 \pm 0.13)}$$

The diameter = diameter of a circle with the same area ( $d_{\text{equ}}$ )

Measure for average 2-grain size = RMS of recrystallized grains

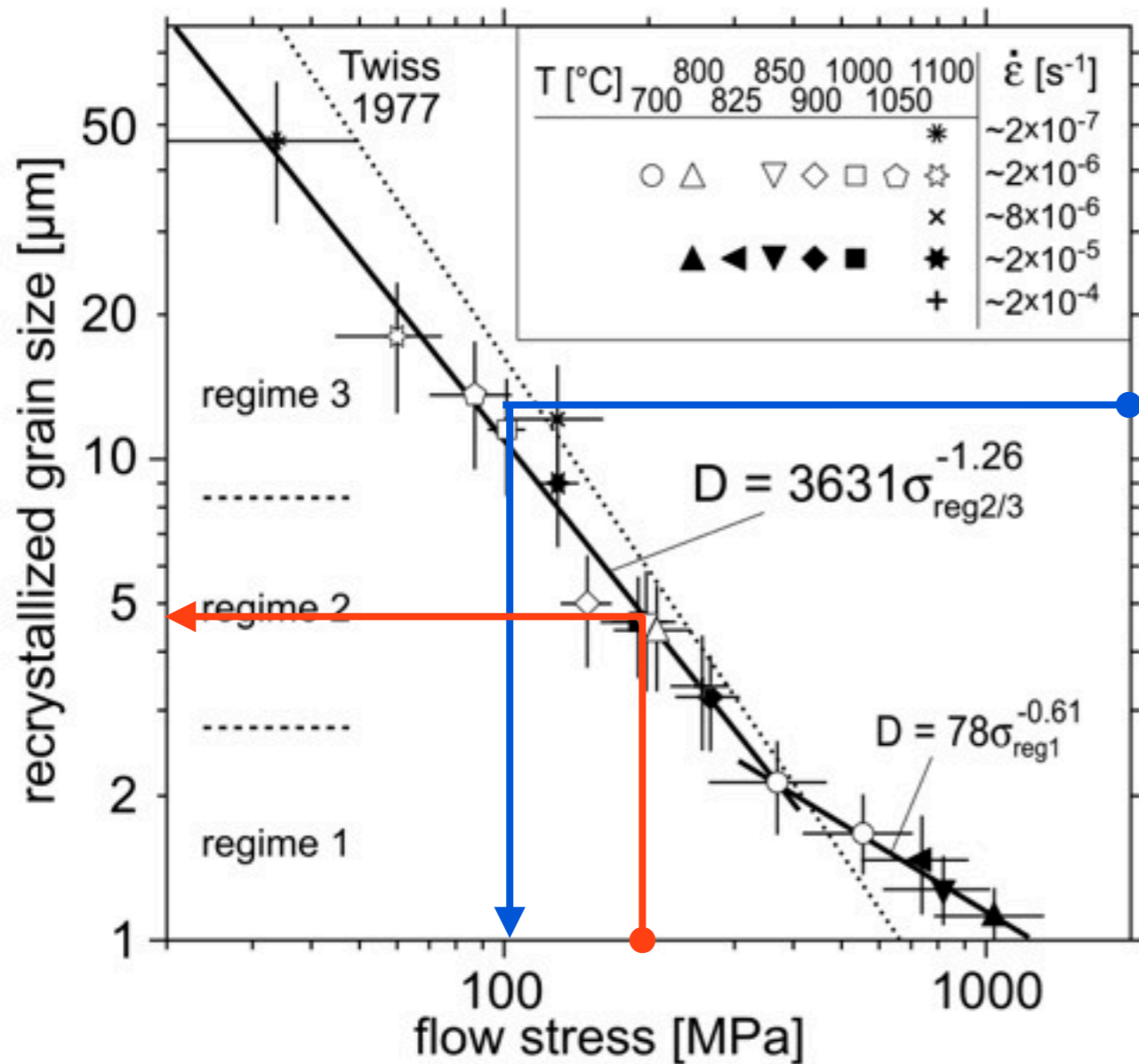
No stereological correction

$$\text{RMS}(d) = 78 \cdot \sigma^{-0.61}$$

(Stipp & Tullis, JGR, 2003)

$\Rightarrow$  piezometer underestimates stress ... or underestimates grain size

# check the piezometer



$$\text{RMS}(d) = 10 (3.56 \pm 0.27) \cdot \sigma^{-(1.26 \pm 0.13)}$$

The diameter = diameter of a circle with the same area ( $d_{\text{equ}}$ )

Measure for average 2-grain size = RMS of recrystallized grains

No stereological correction

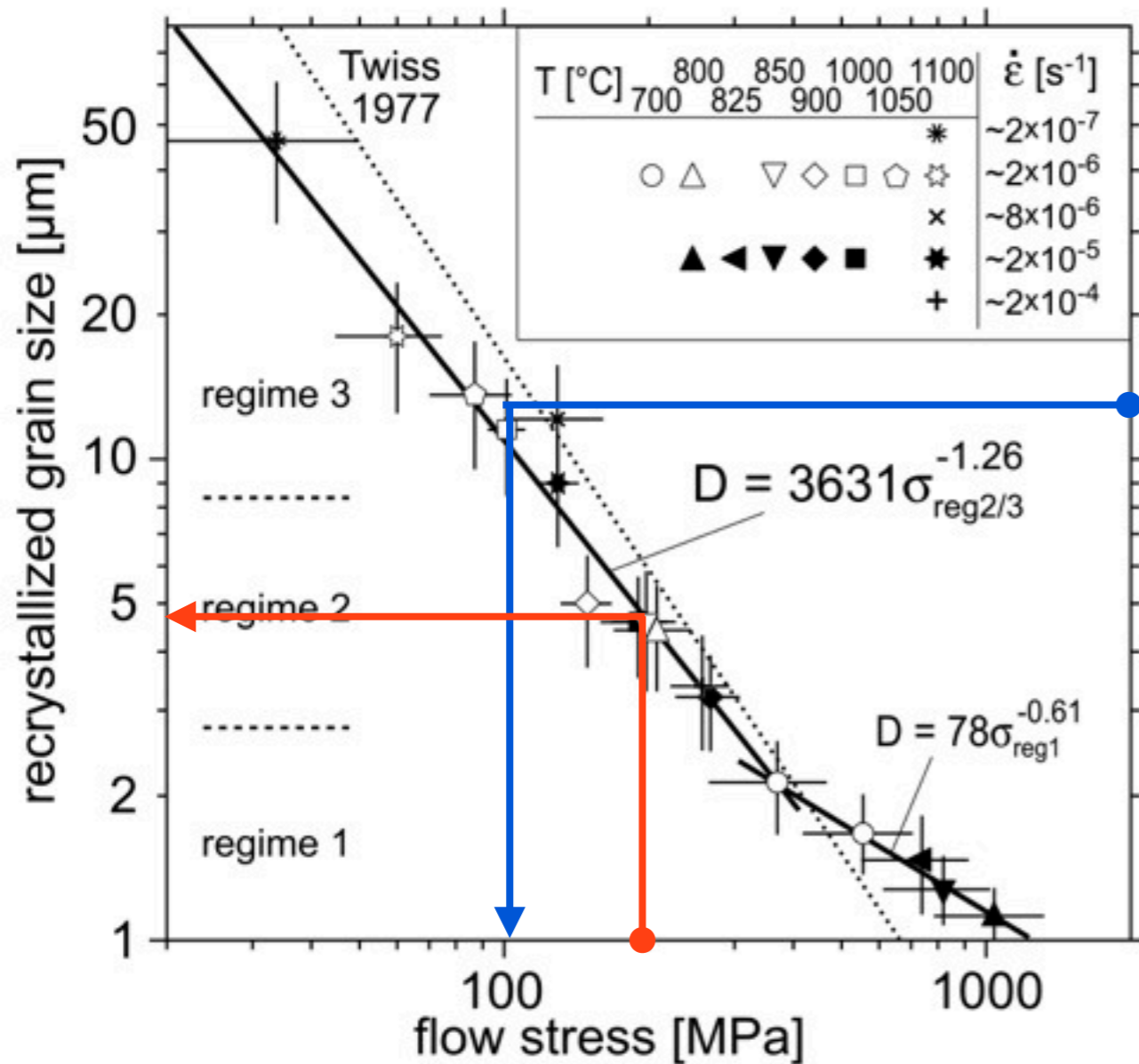
$$\text{RMS}(d) = 78 \cdot \sigma^{-0.61}$$

(Stipp & Tullis, JGR, 2003)

$$\tau = 100 \text{ MPa} \rightarrow \Delta\sigma = 200 \text{ MPa} \rightarrow d = 4.6 \text{ } \mu\text{m}$$

$\Rightarrow$  piezometer underestimates stress ... or underestimates grain size

# check the piezometer



$$\text{RMS}(d) = 10 (3.56 \pm 0.27) \cdot \sigma^{-(1.26 \pm 0.13)}$$

The diameter = diameter of a circle with the same area ( $d_{\text{equ}}$ )

Measure for average 2-grain size = RMS of recrystallized grains

No stereological correction

$$\text{RMS}(d) = 78 \cdot \sigma^{-0.61}$$

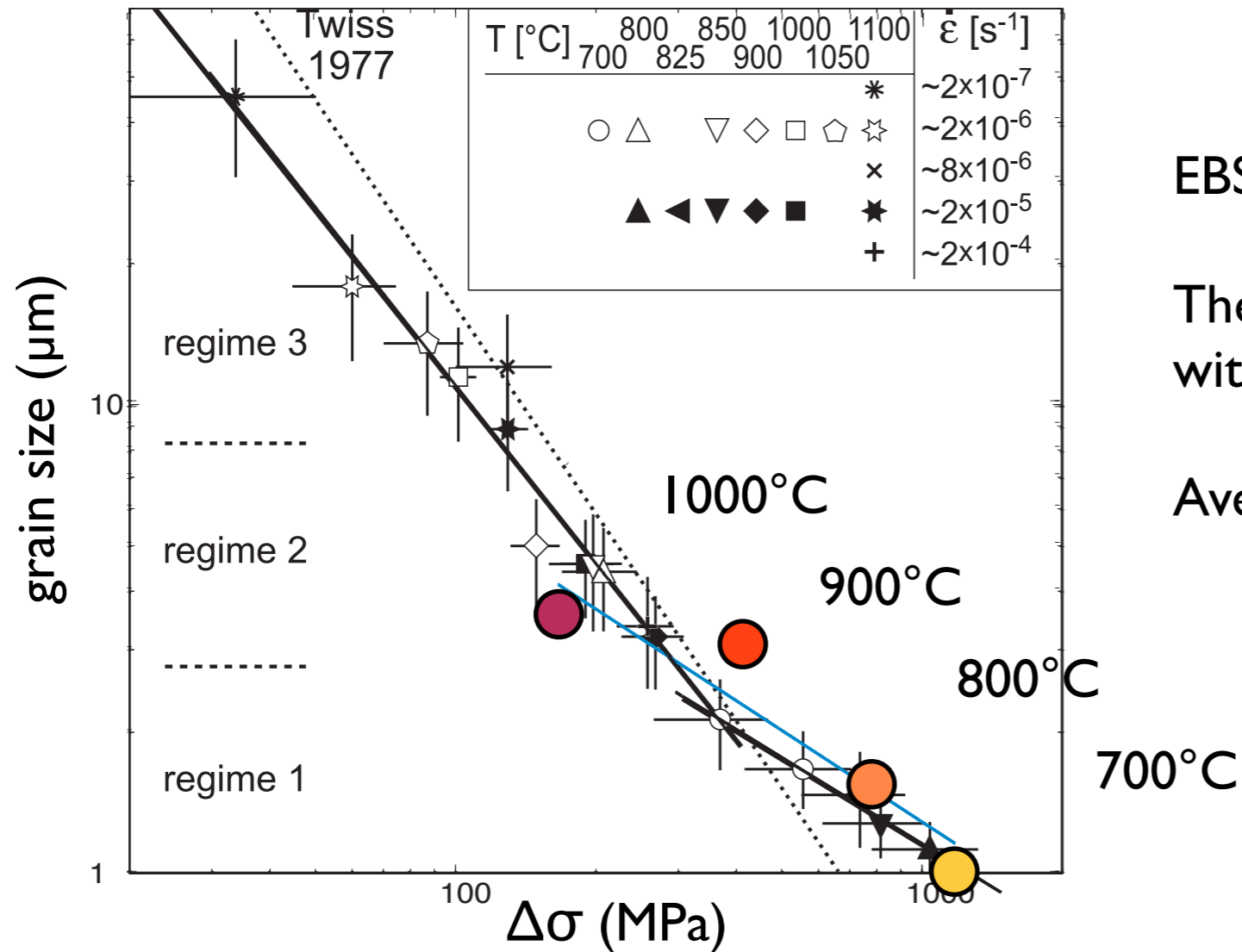
(Stipp & Tullis, JGR, 2003)

$$\tau = 100 \text{ MPa} \rightarrow \Delta\sigma = 200 \text{ MPa} \rightarrow d = 4.6 \text{ } \mu\text{m}$$

$$d = 10 \text{ } \mu\text{m} \rightarrow \Delta\sigma = 108 \text{ MPa} \rightarrow \tau = 54 \text{ MPa}$$

$\Rightarrow$  piezometer underestimates stress ... or underestimates grain size

# check stresses (= work in progress)



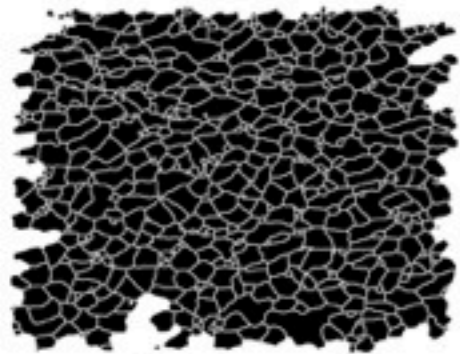
EBSD maps were used

The diameter = diameter of a circle with the same area.

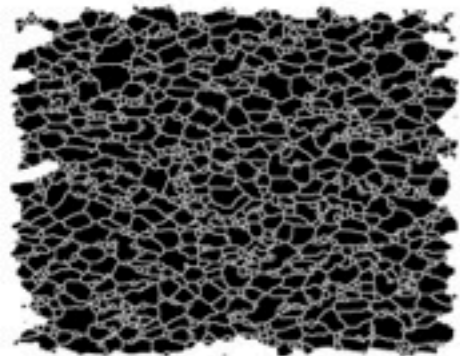
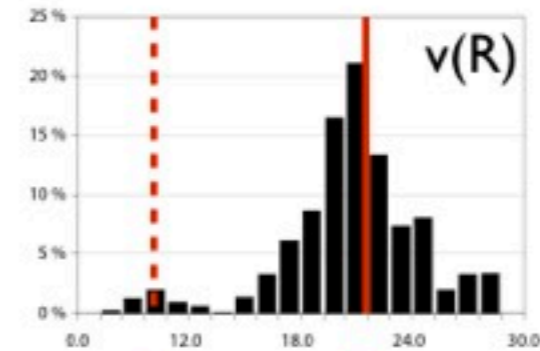
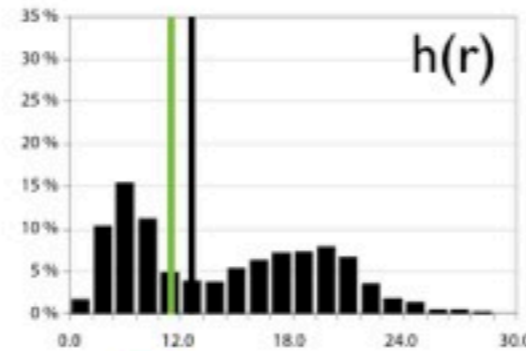
Average grain size = mode of  $h(d_{\text{equ}})$ .

$\Rightarrow$  re-calibrate the Griggs apparatus

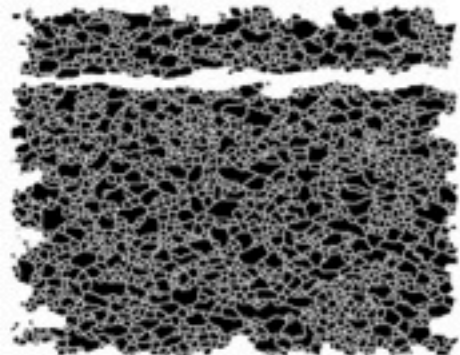
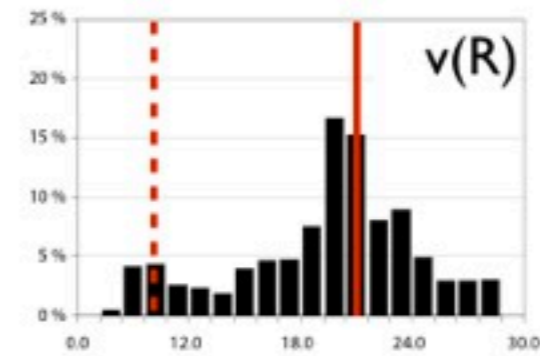
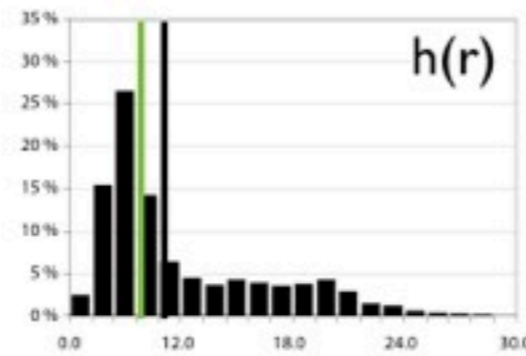
# use 3D mode(s) (= my mission on earth..)



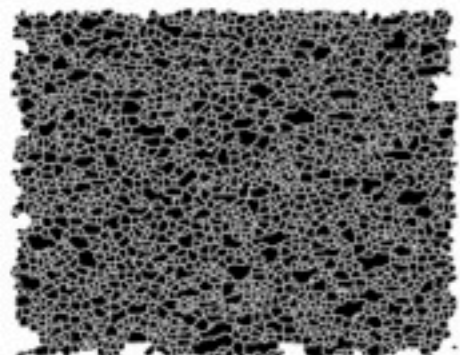
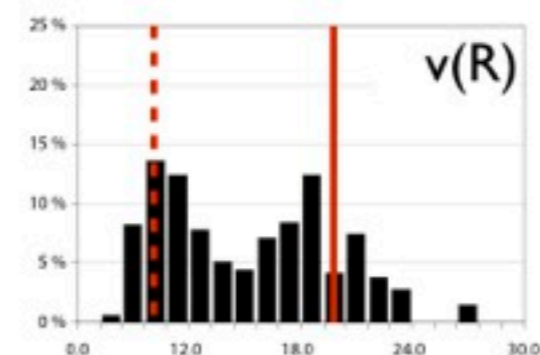
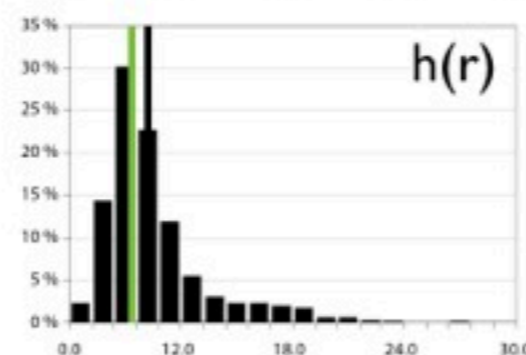
mean  $r_{equ}$  = 10.5px  
RMS = 12.4px  
RMS/mean = 118%



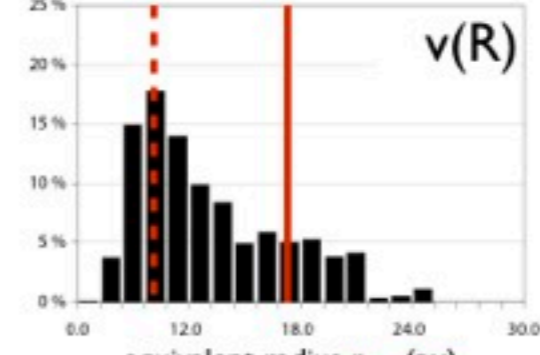
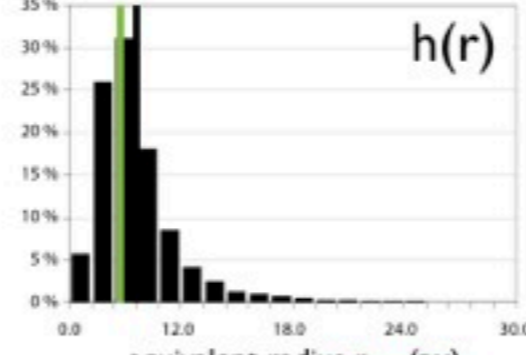
mean  $r_{equ}$  = 7.6px  
RMS = 9.5px  
RMS/mean = 125%



mean  $r_{equ}$  = 5.7px  
RMS = 6.7px  
RMS/mean = 118%



mean  $r_{equ}$  = 4.5px  
RMS = 5.2px  
RMS/mean = 117%



⇒ 3D mode more meaningful than 2D mean



## 2. olivine - pyroxene (= work in progress)

motivation:

torsion experiments to find flow law for mantle material

first finds:

dislocation creep and diffusion creep

aim of microstructure analysis:

step 1: find grain size(s) of olivine and pyroxene

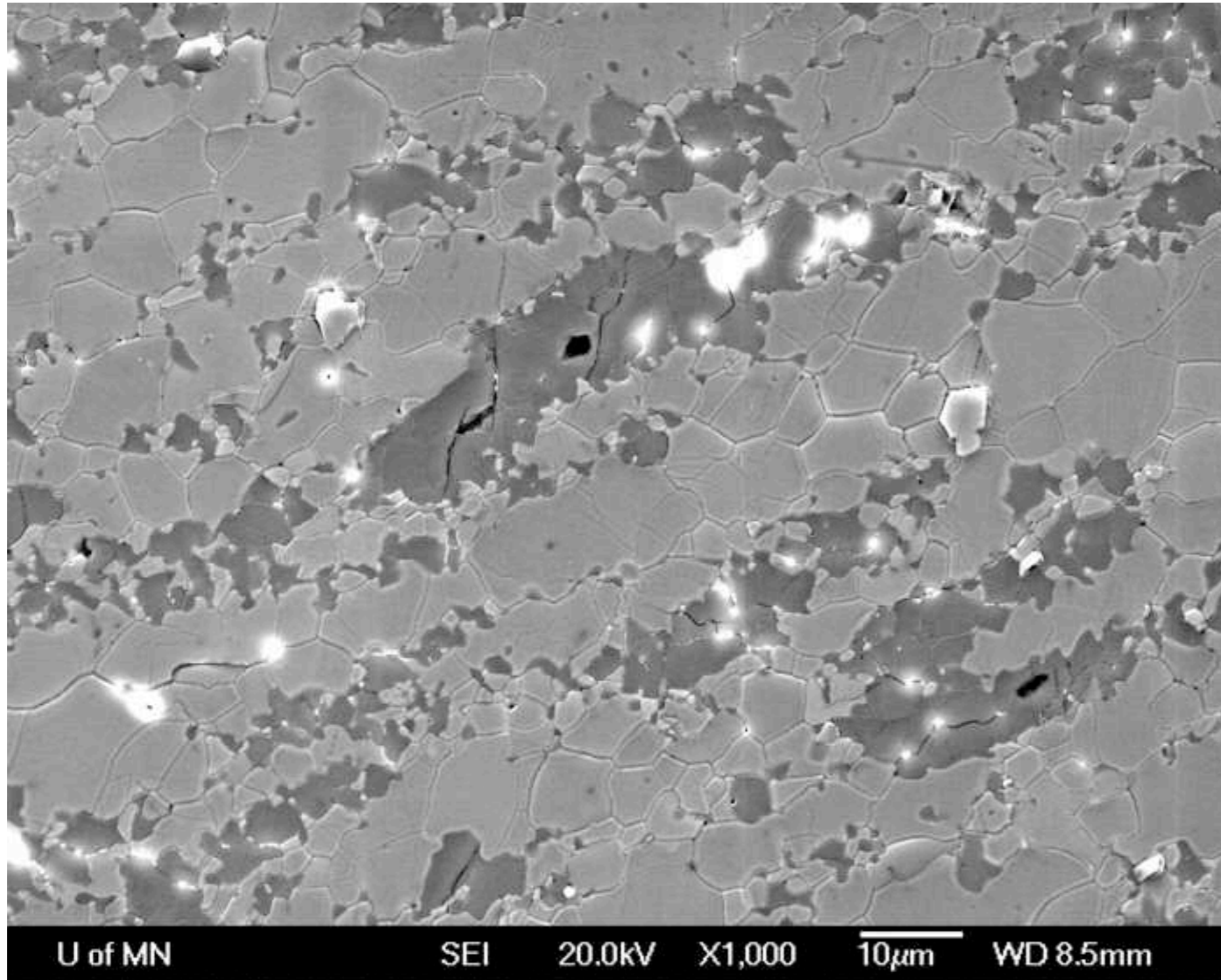
step 2: find shape(s)

step 3: find spatial relations

... think about results

... see forthcoming paper by Miki Tasaka

# torsion experiments on Ol - Opx



Miki Tasaka  
David Kohlstedt  
Mark Zimmermann

Univ. Minnesota, Minneapolis

70:30 mixture  
olivine-orthopyroxene

Paterson apparatus

$T = 1200^{\circ}\text{C}$

$p_c = 300\text{MPa}$

$\dot{\gamma} = 1.6 \cdot 10^{-4} \text{ s}^{-1}$

$\gamma = 1.9$

# torsion experiments on Ol - Opx



segmentation

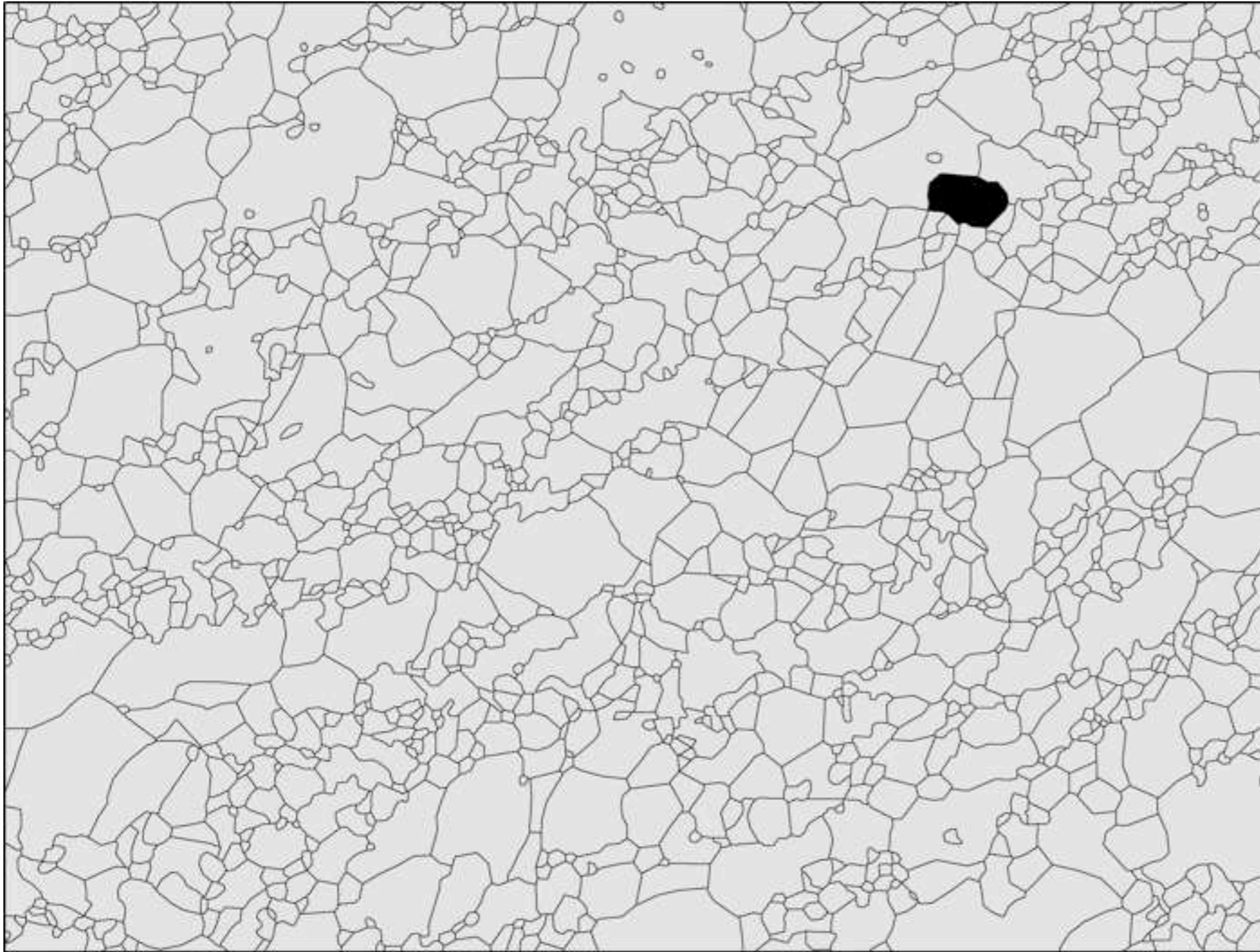
□ olivine

■ orthopyroxene

■ all grains

⇒ *have to be careful with segmentation*

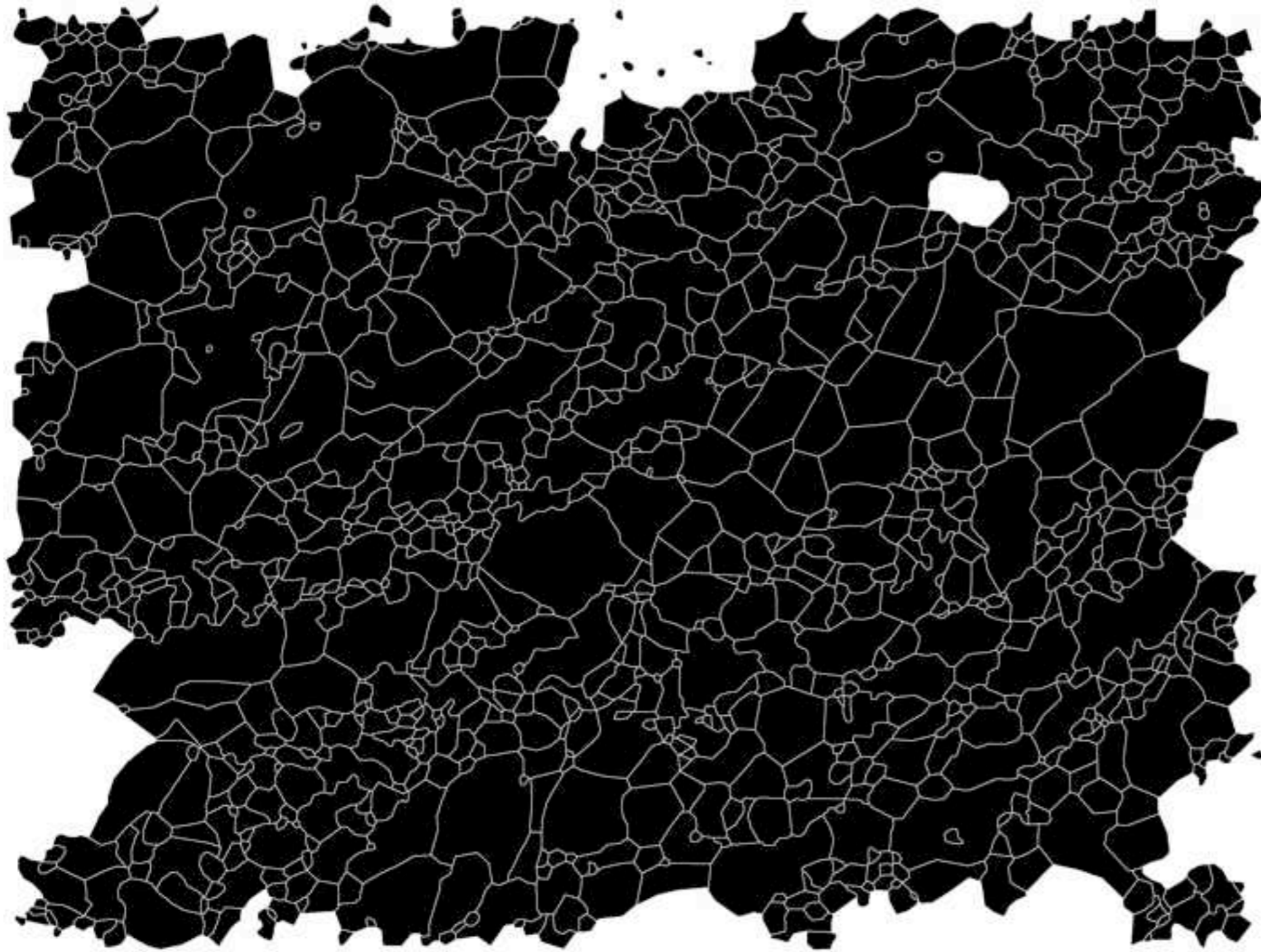
# torsion experiments on Ol - Opx



segmentation  
grain boundary map

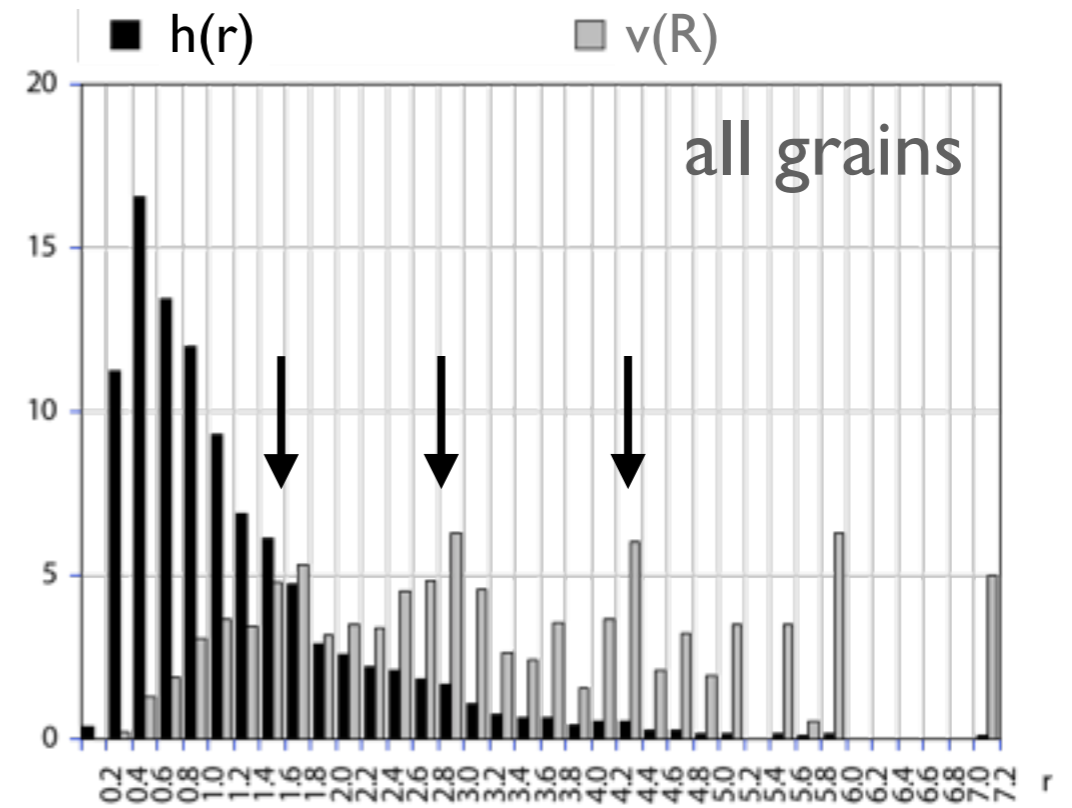
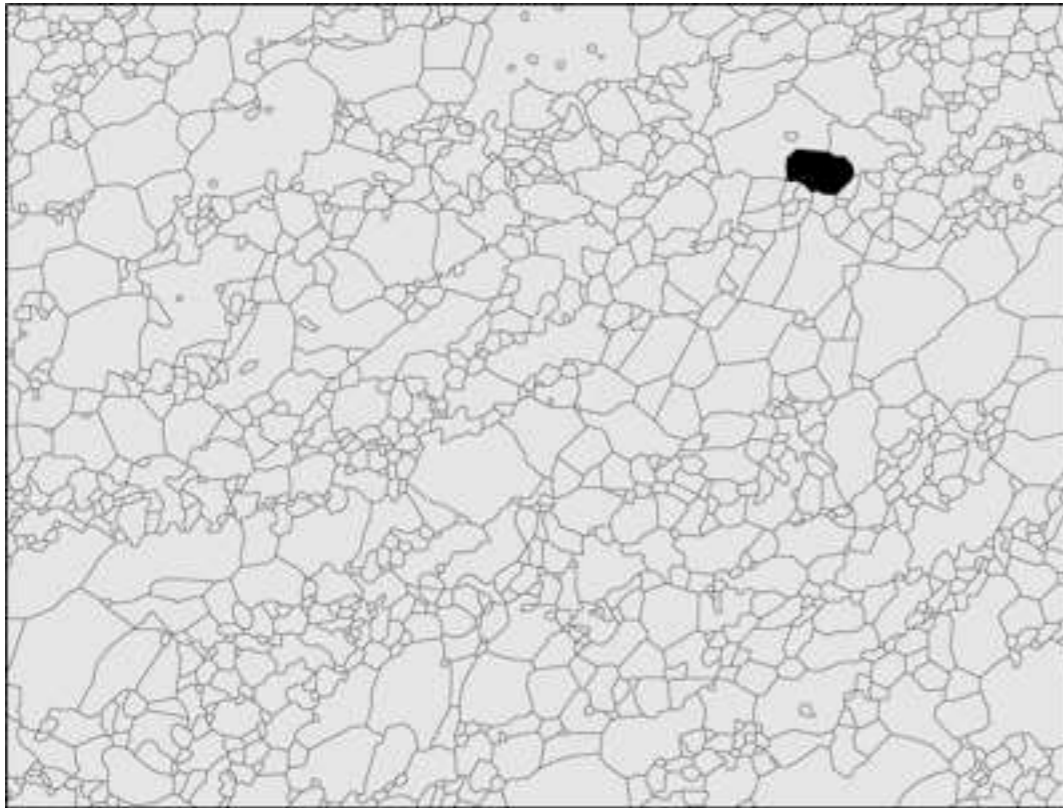
□ all grains

# torsion experiments on Ol - Opx



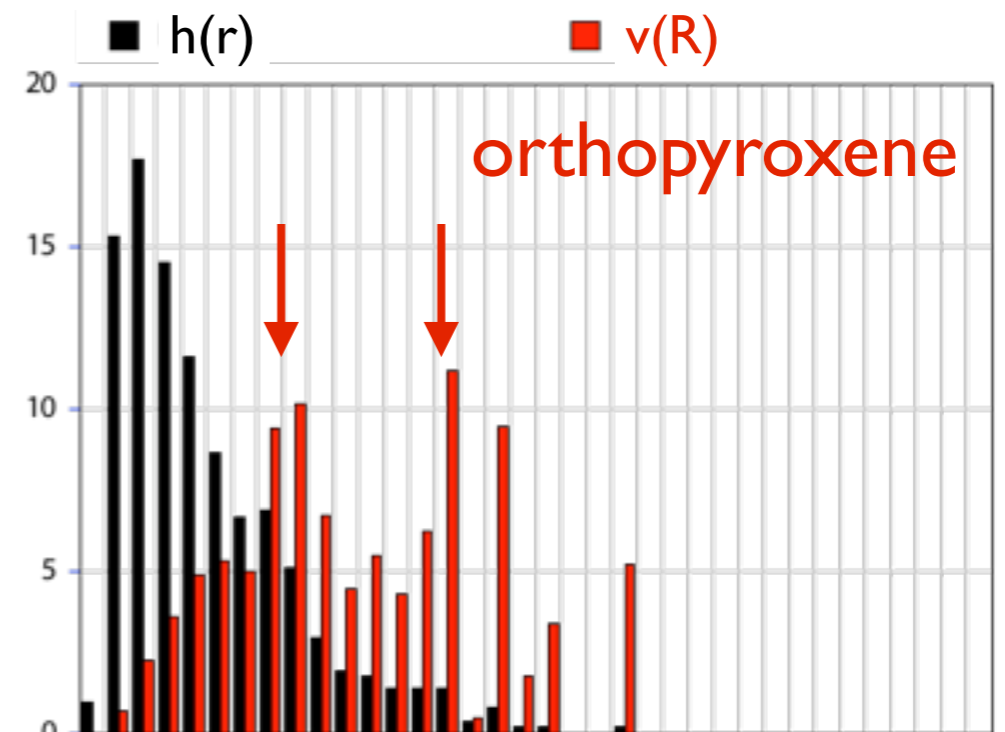
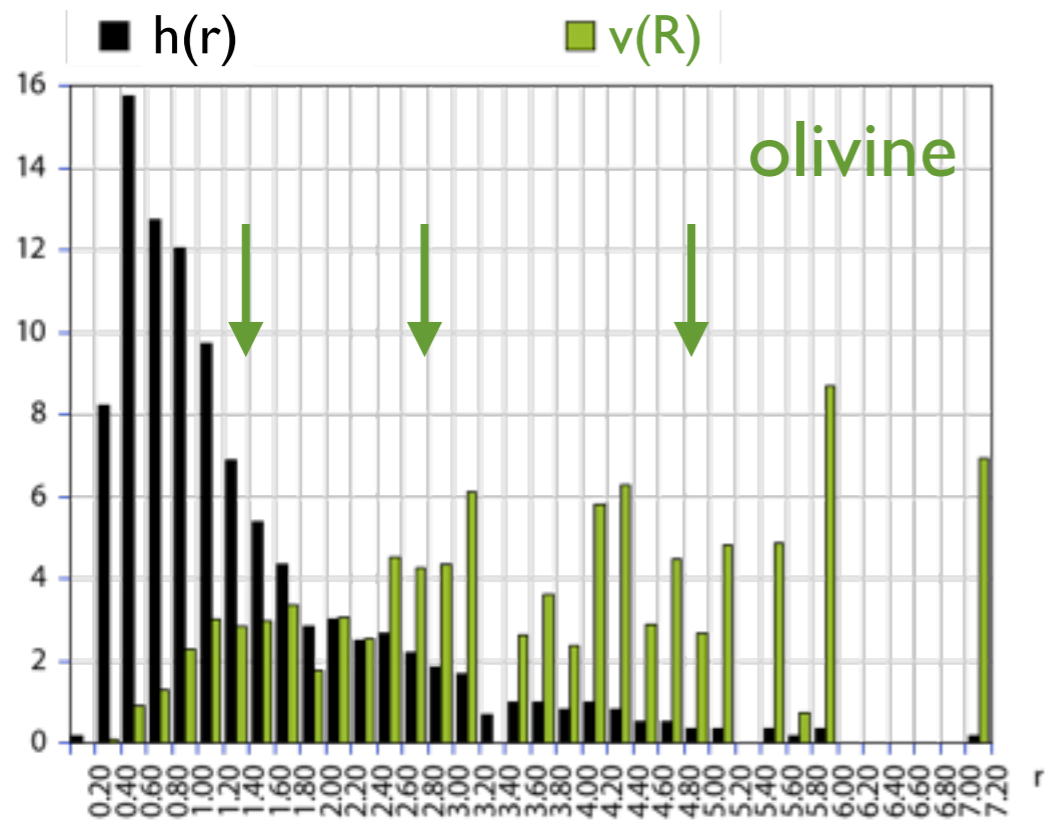
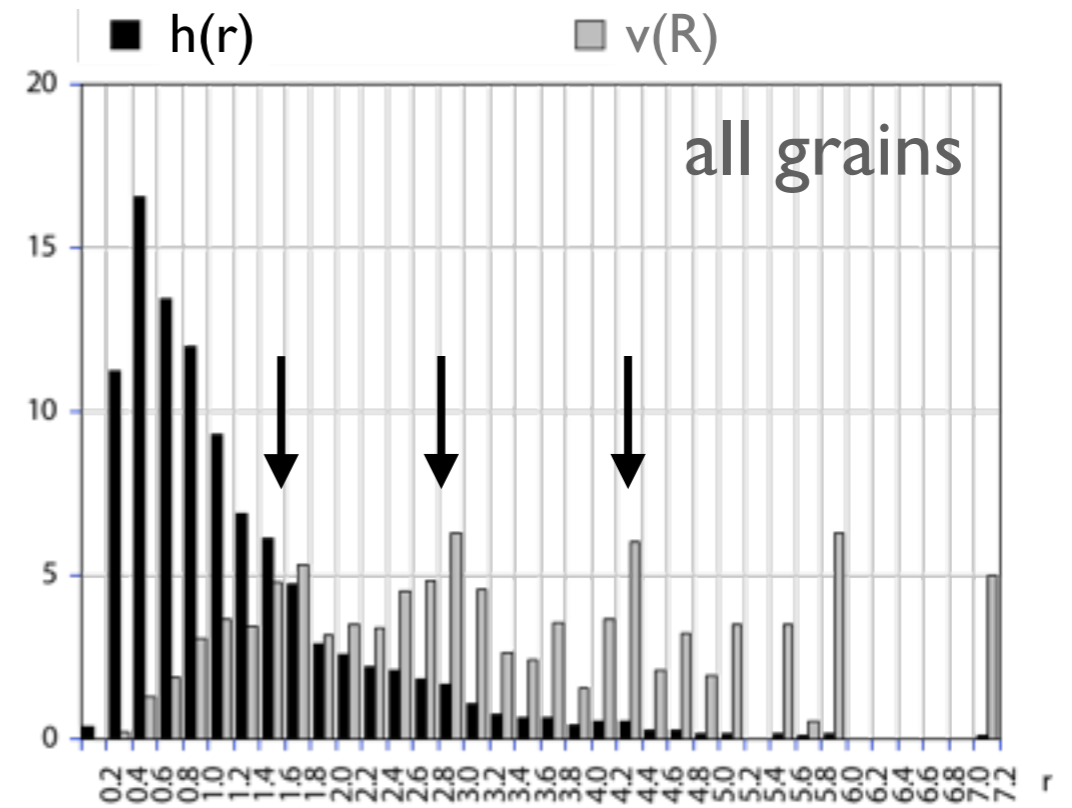
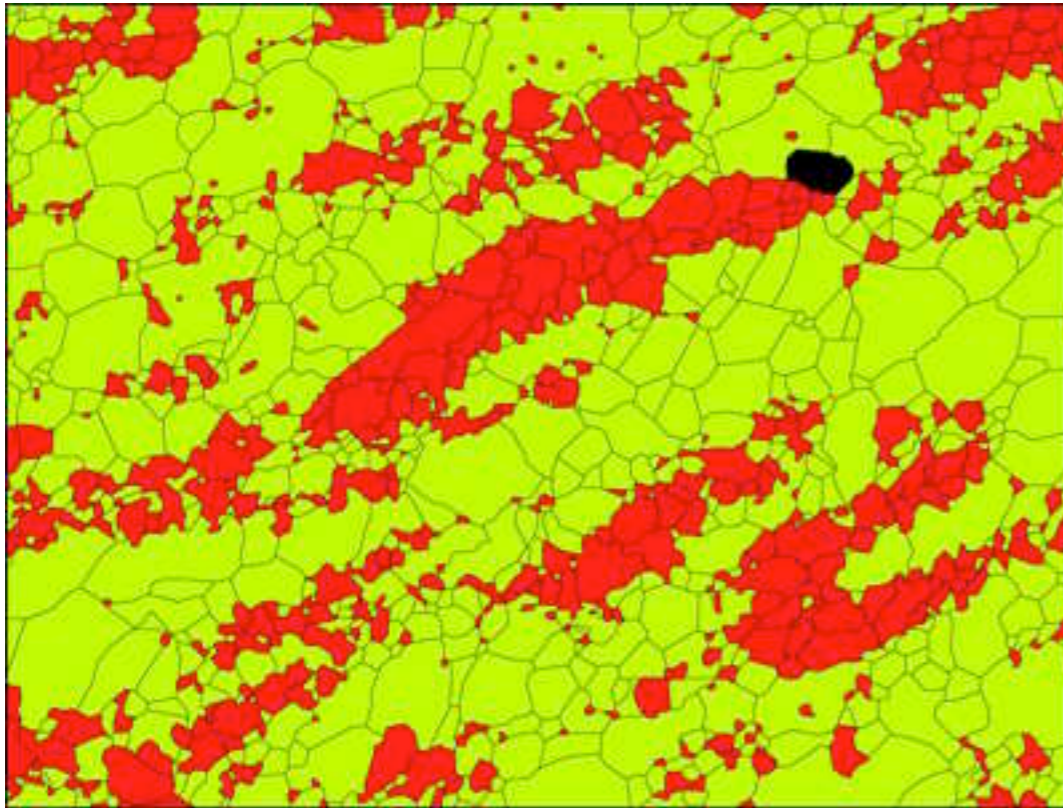
segmentation  
grain boundary map  
grain map (segments)

# 2D and 3D grain size distributions



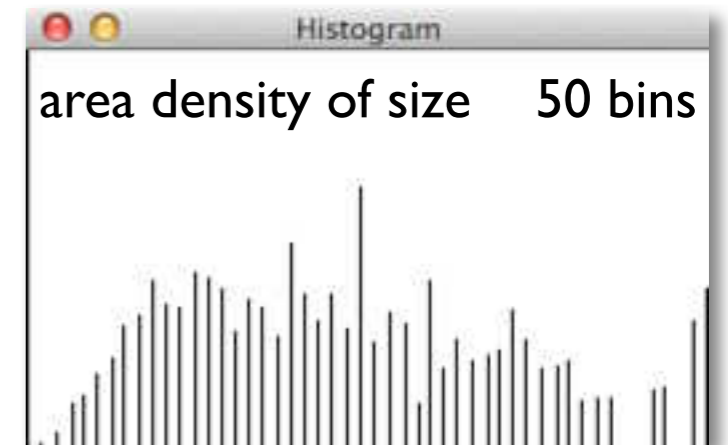
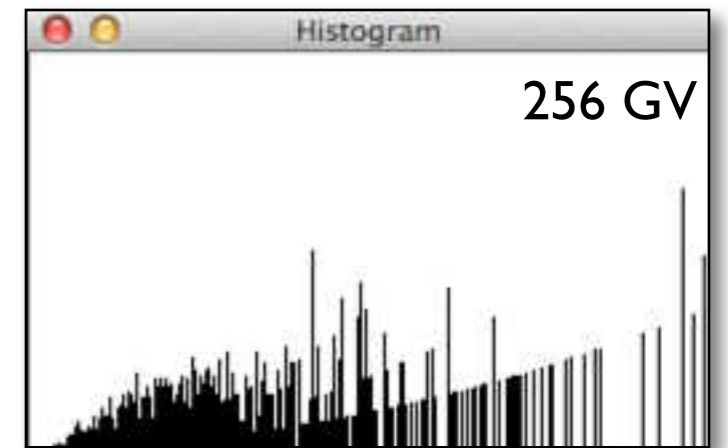
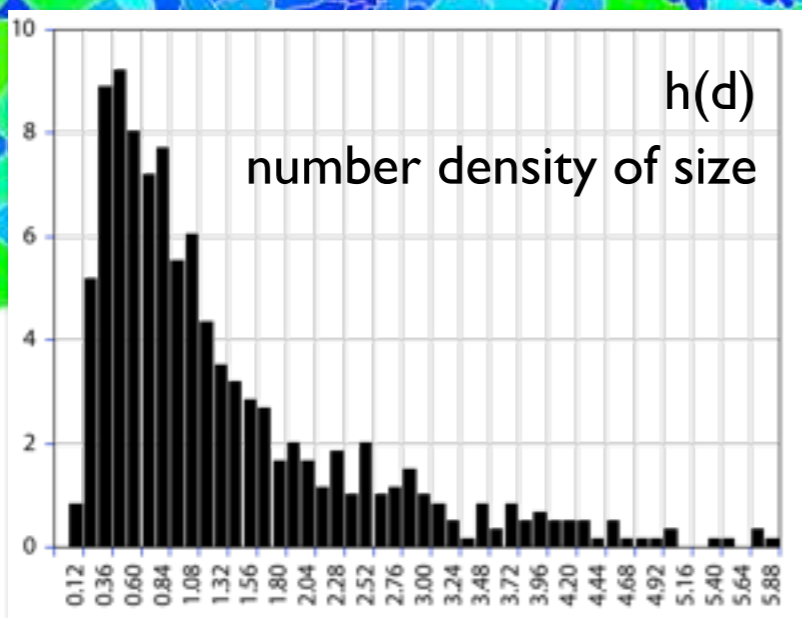
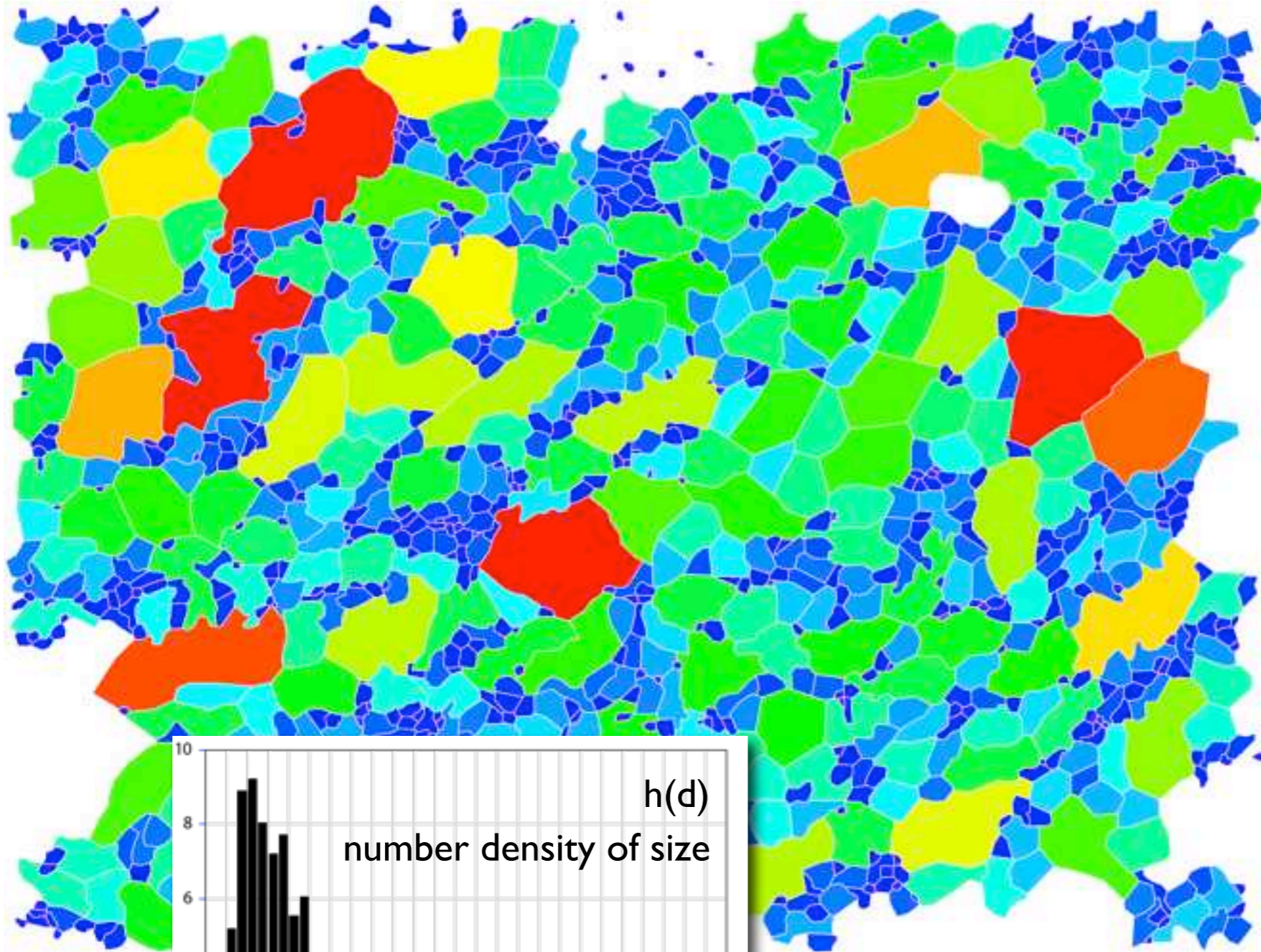
⇒ *detect multiple modes in 3D*

# 2D and 3D grain size distributions



$\Rightarrow$  detect multiple modes in 3D

# grain size mapping



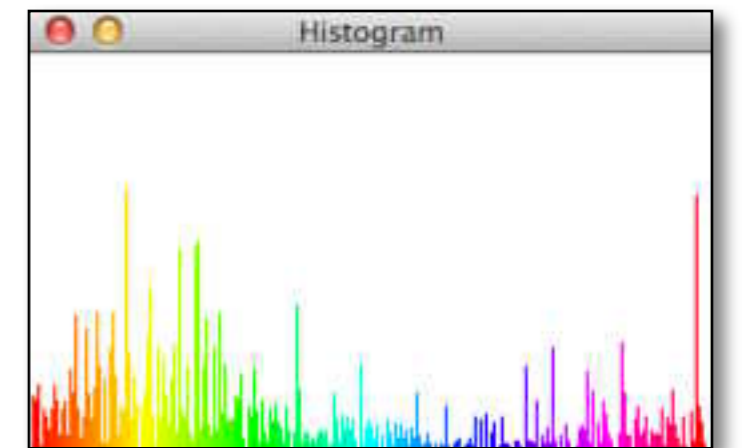
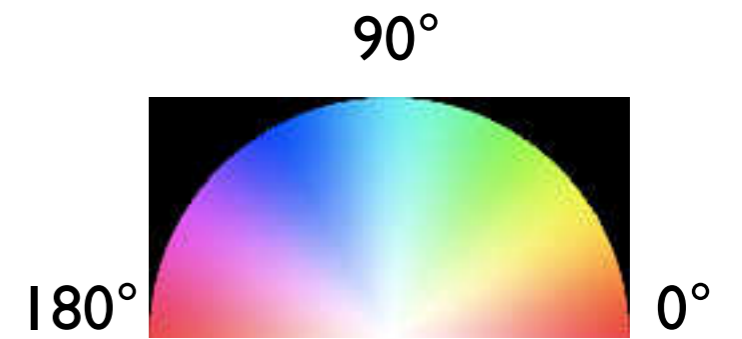
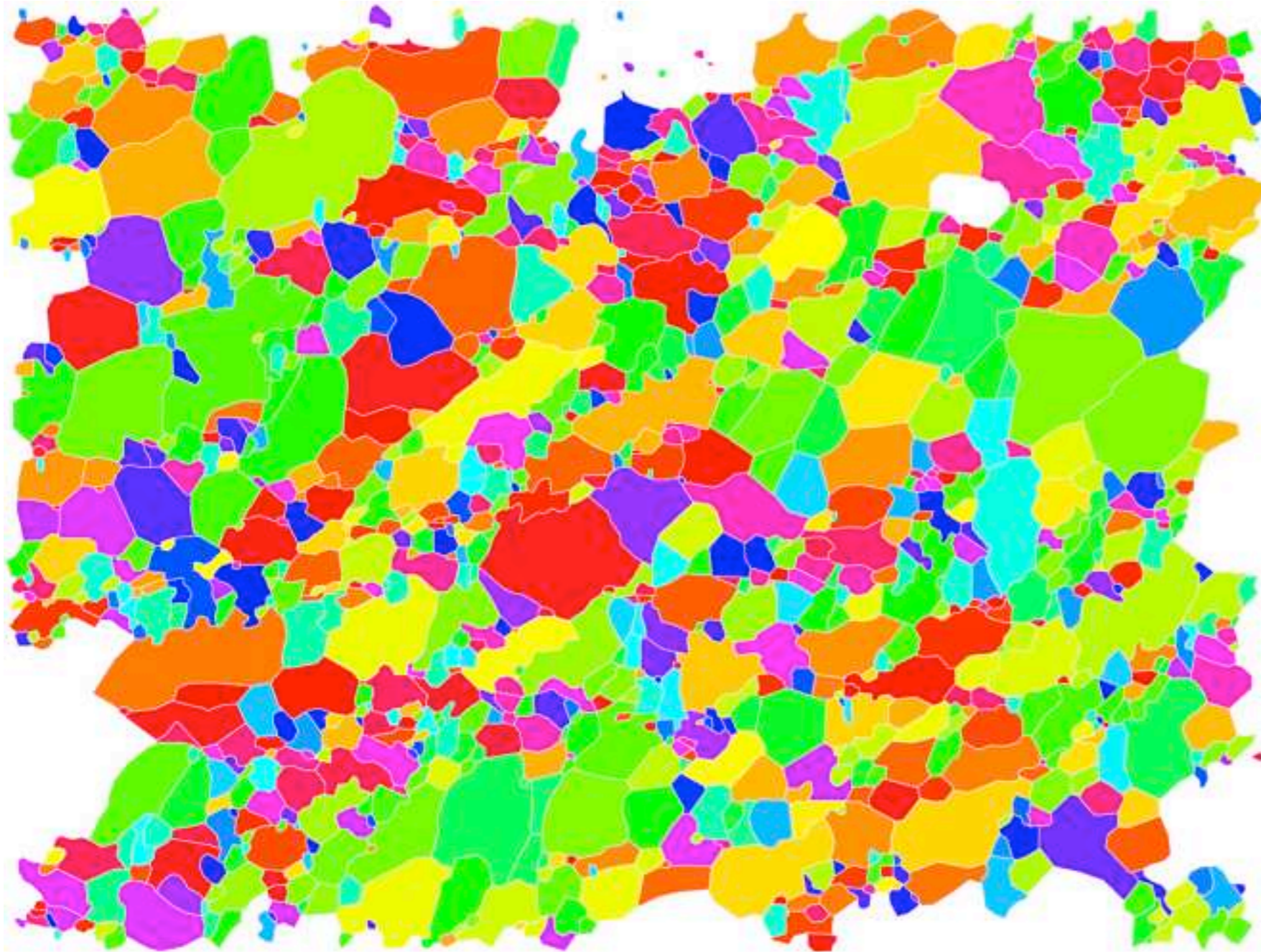
0.0  $r_{\text{equ}}$  ( $\mu\text{m}$ ) 6.0

0.0  $d_{\text{equ}}$  ( $\mu\text{m}$ ) 12.0

$\Rightarrow$  size domains

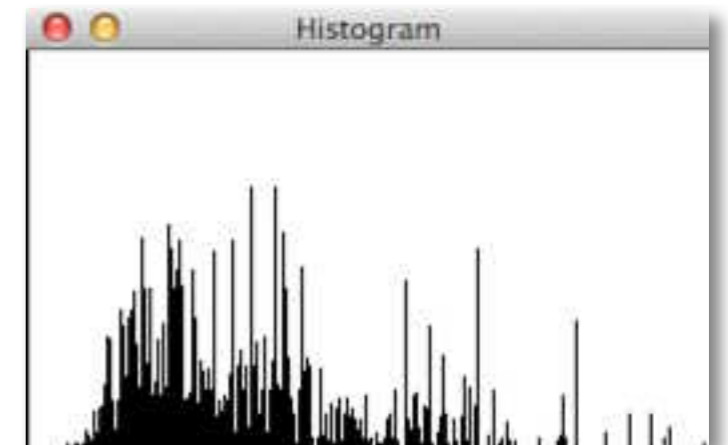
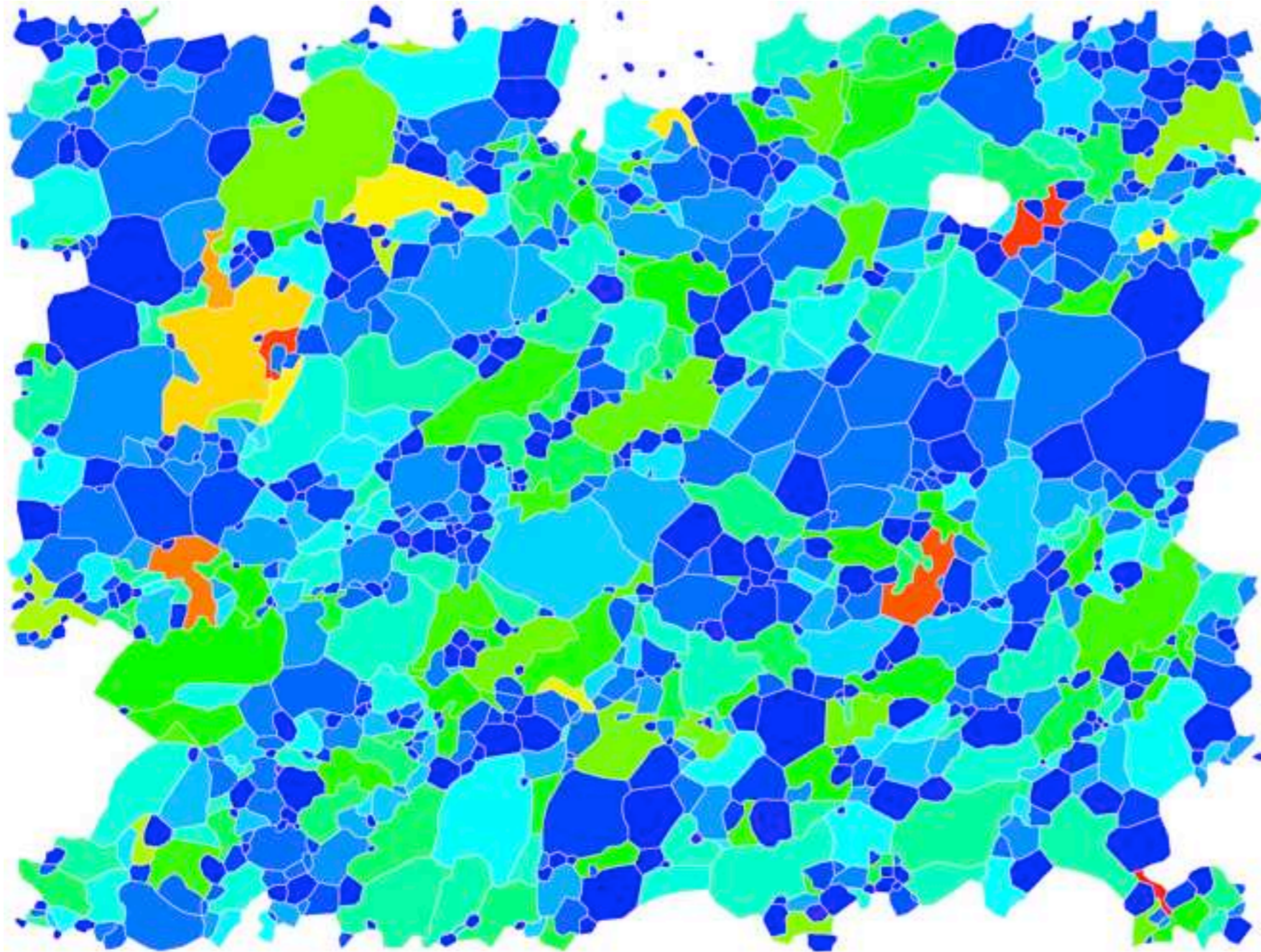


# orientation mapping



⇒ *random orientation*

# shape factor mapping



0.0

$P/P_{\text{equ}}$

2.0

round  
convex



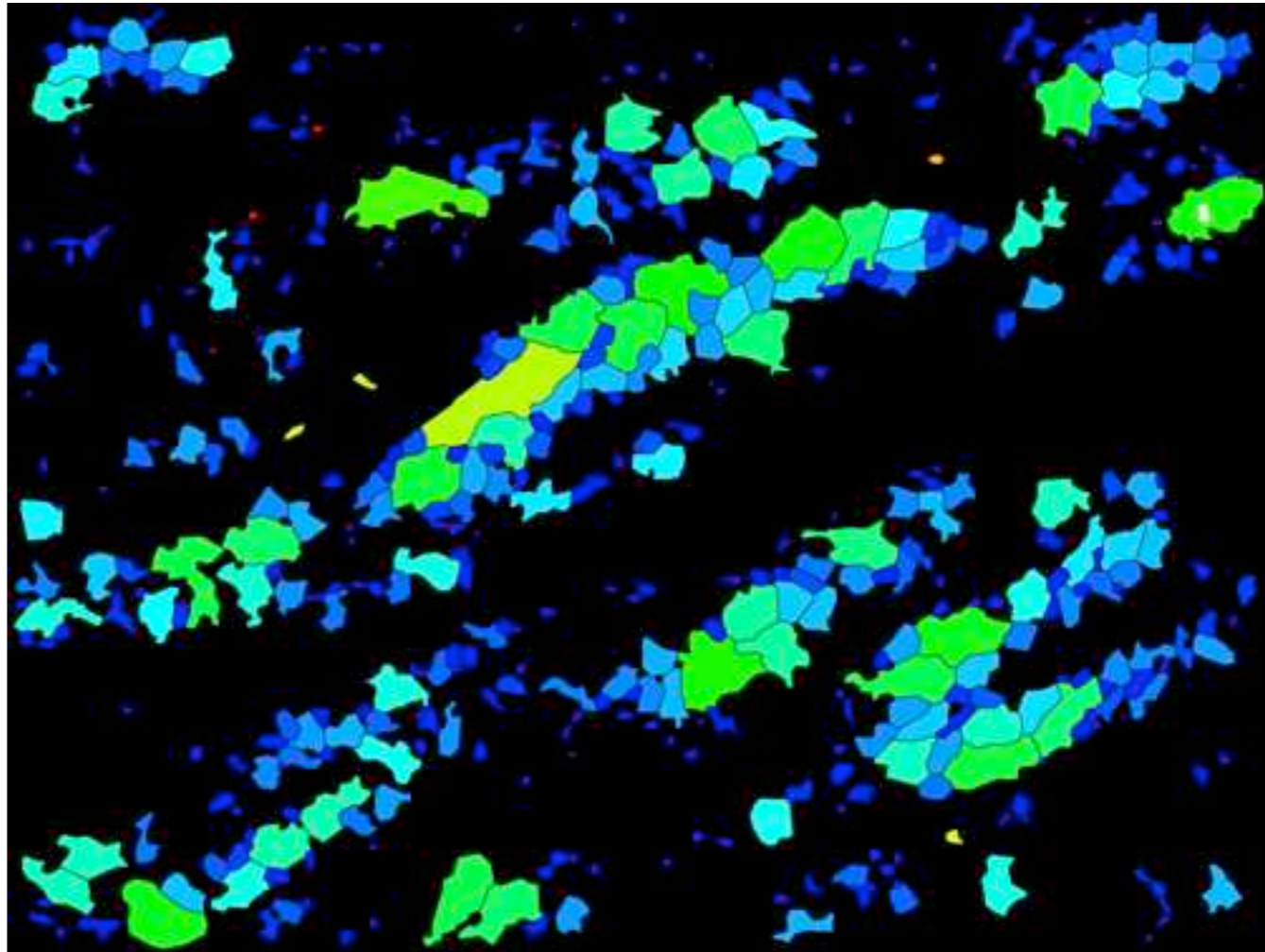
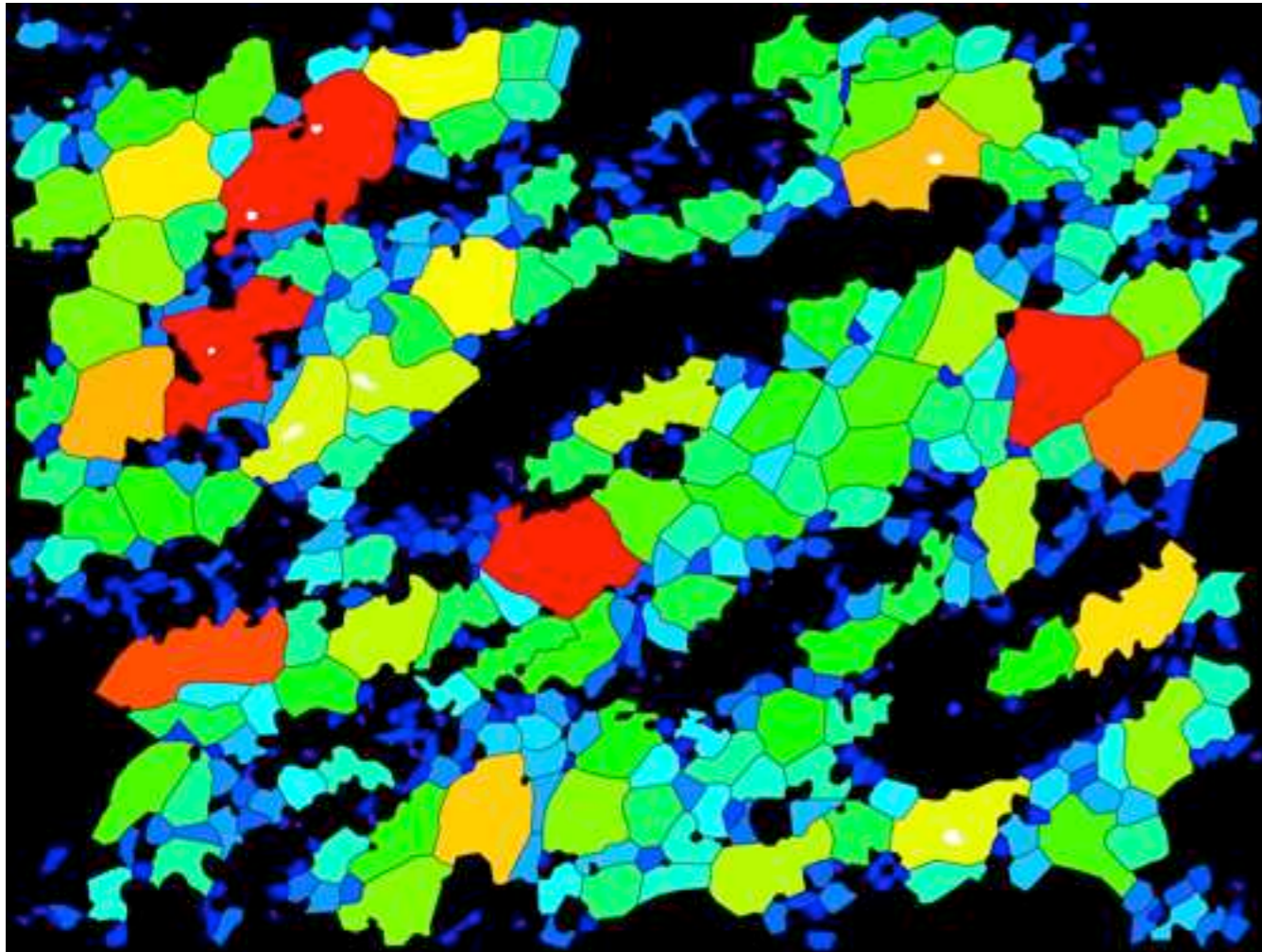
elongate  
convex-concave

$SFI = P_{\text{measured}} / P_{\text{equivalent}} = \text{large if grain boundary lobate}$

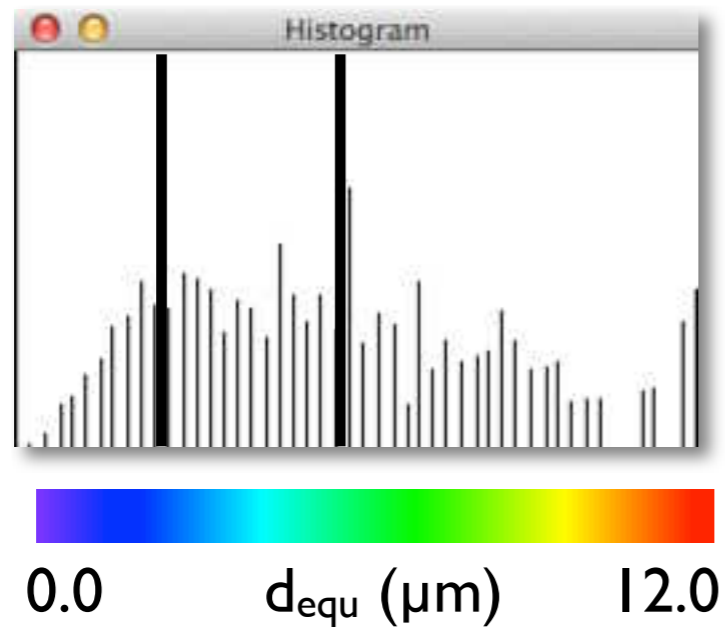
$(0.00 < SFI < \infty)$

$(0.00 < SFI < \infty)$

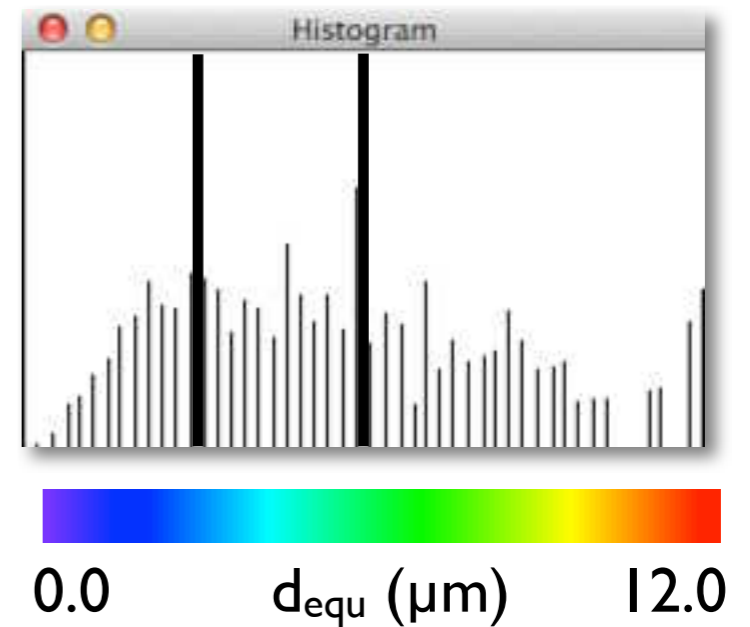
# 2 phases - 4 grain sizes !



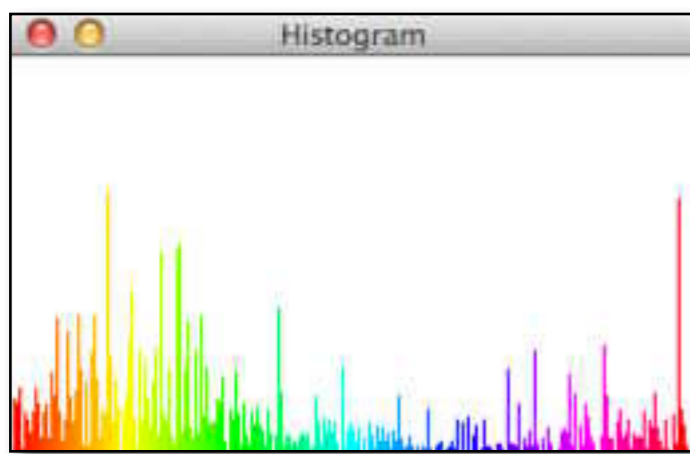
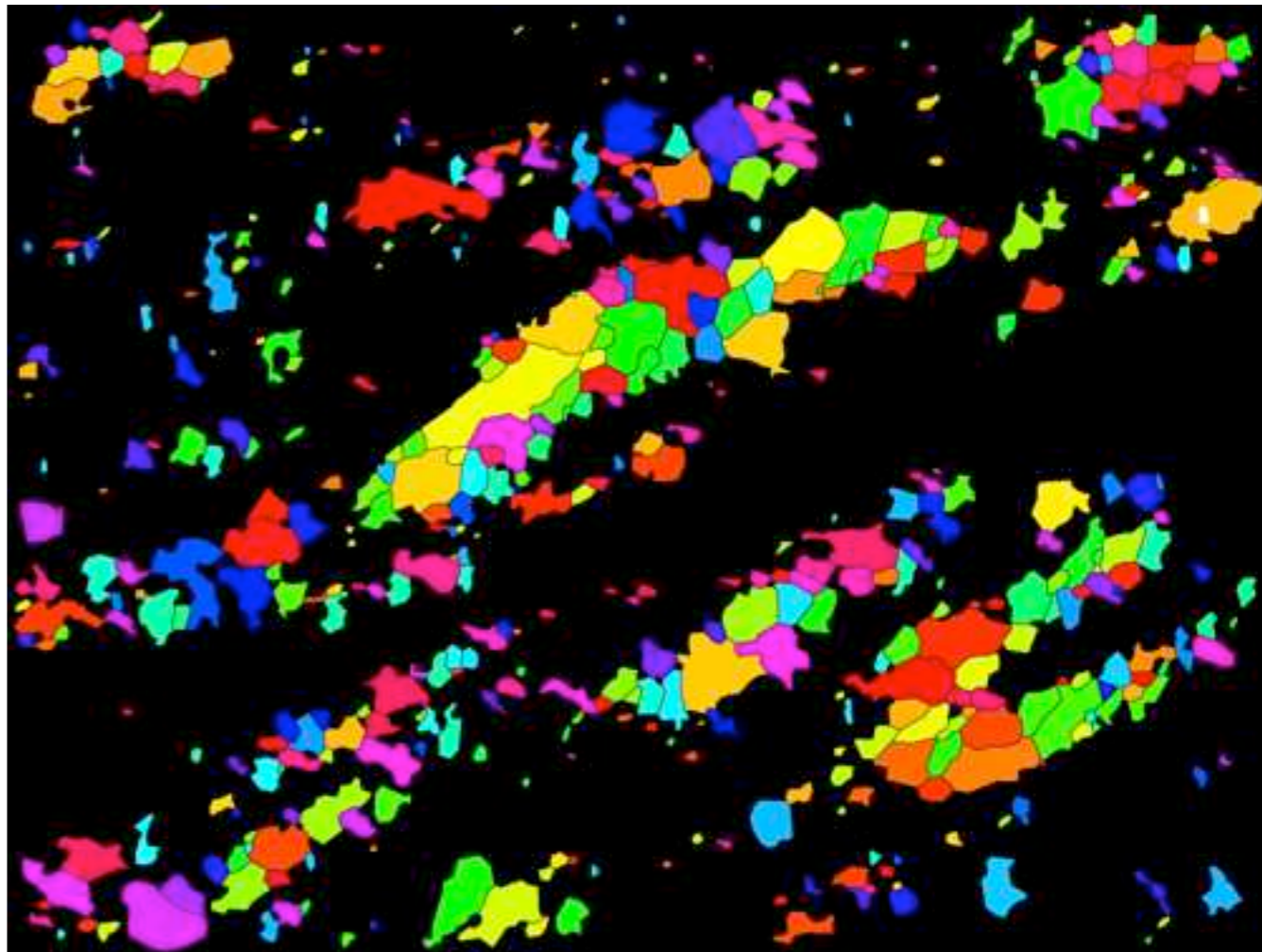
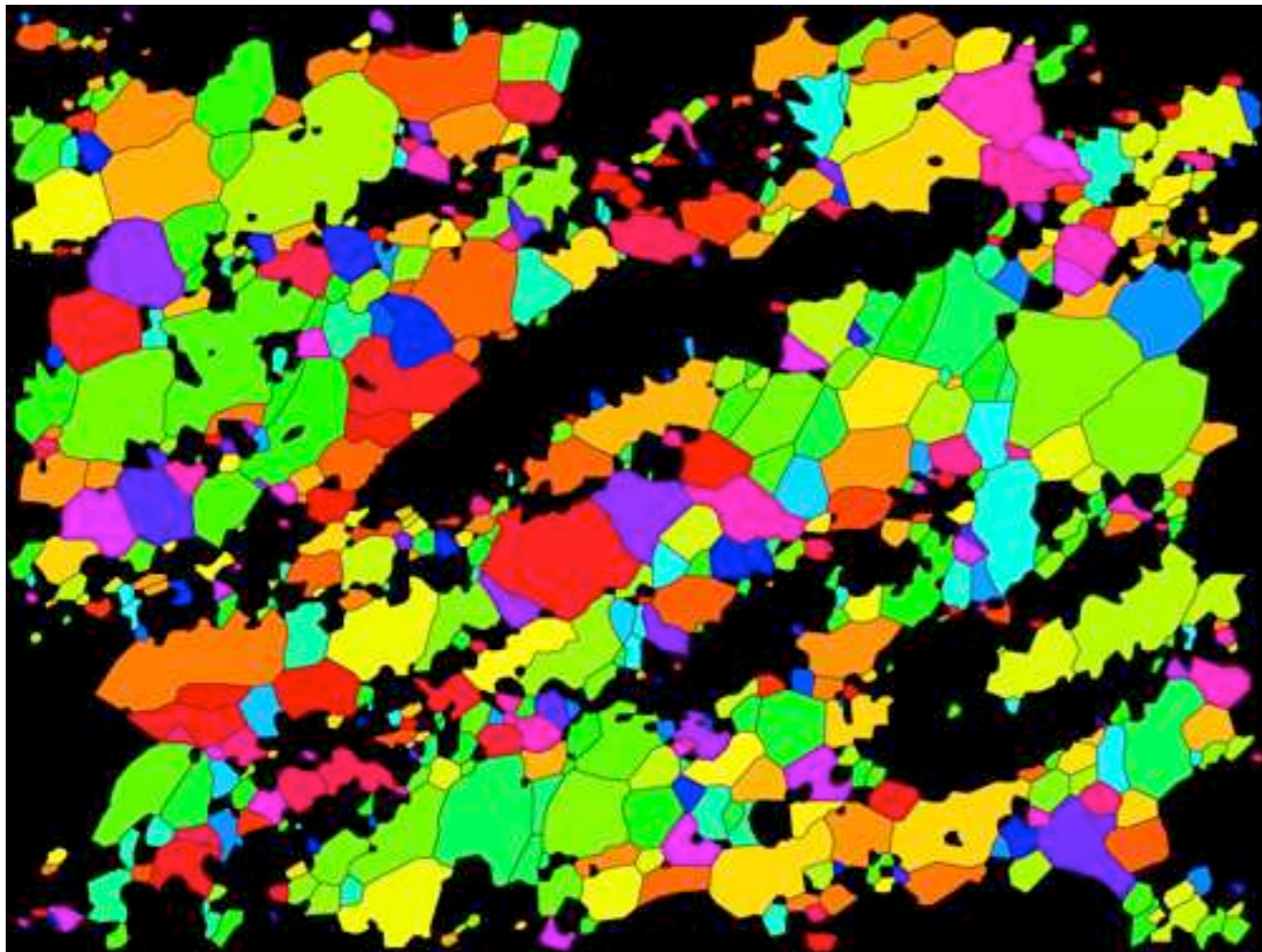
ol



opx

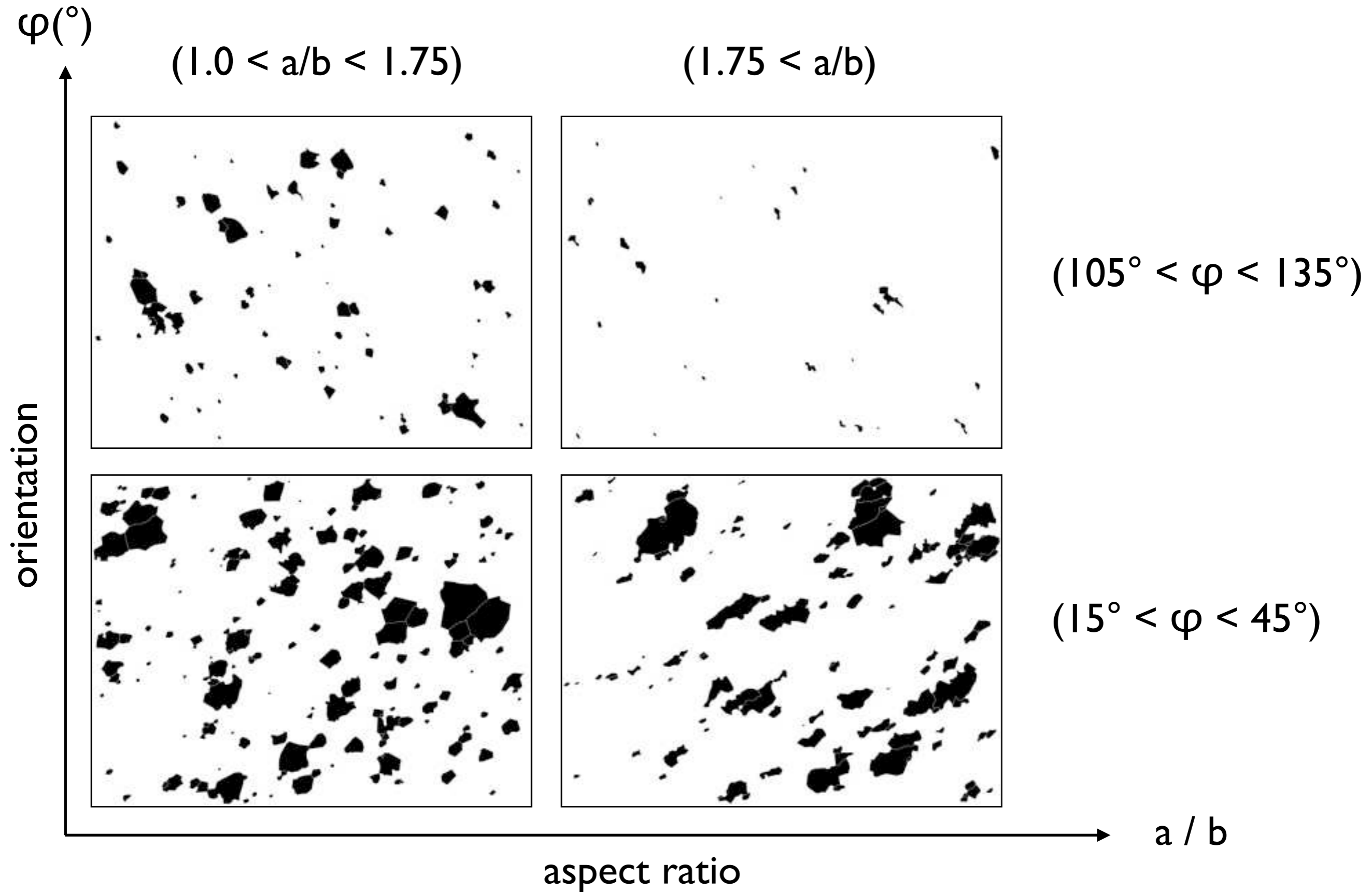


# preferred orientation ?



⇒ *Ol and Opx = random orientation*

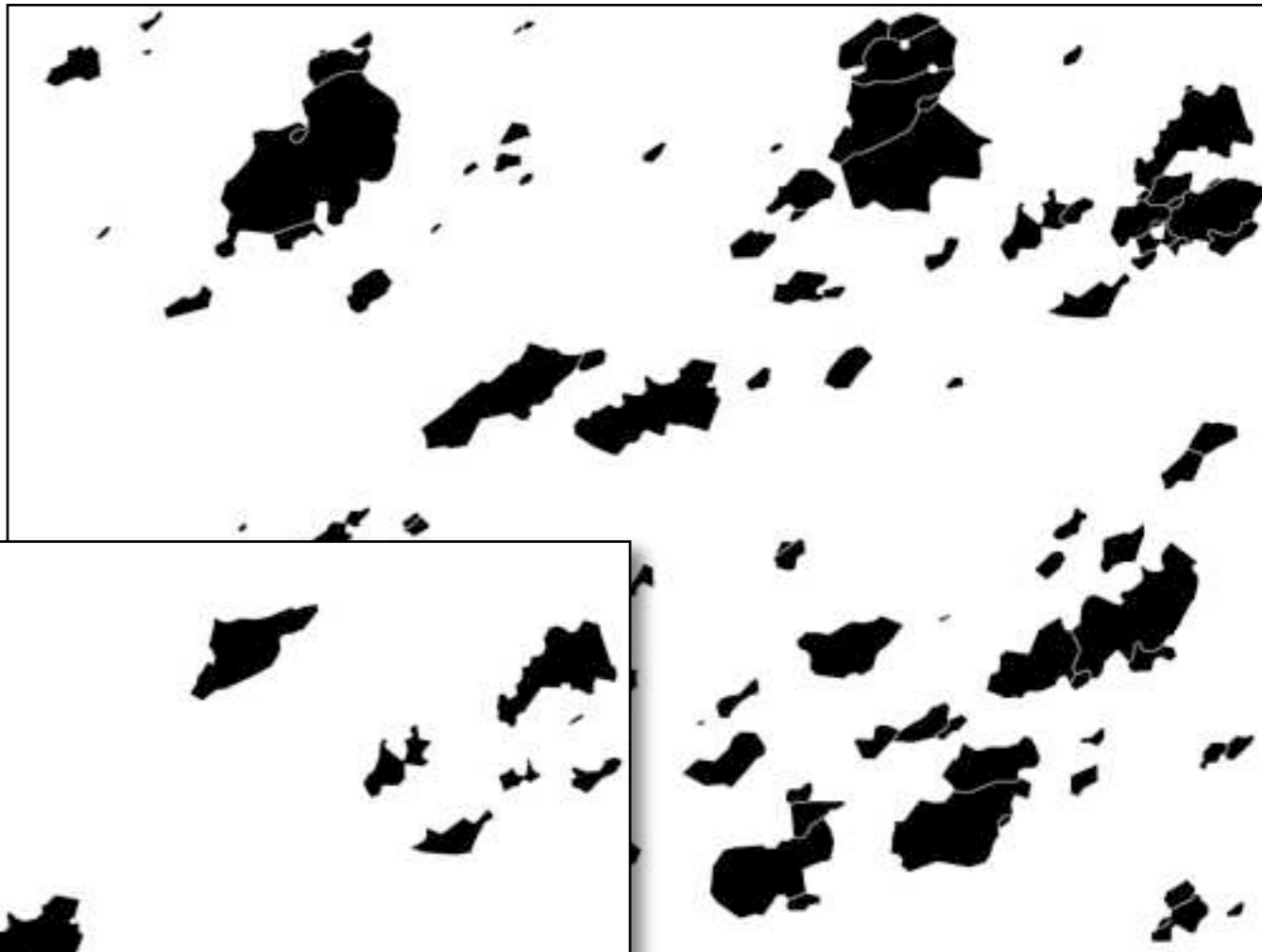
# intersecting 2 feature bitmaps



# intersecting 3 feature bitmaps



$(1.5 < \text{SFI} < 2.0)$

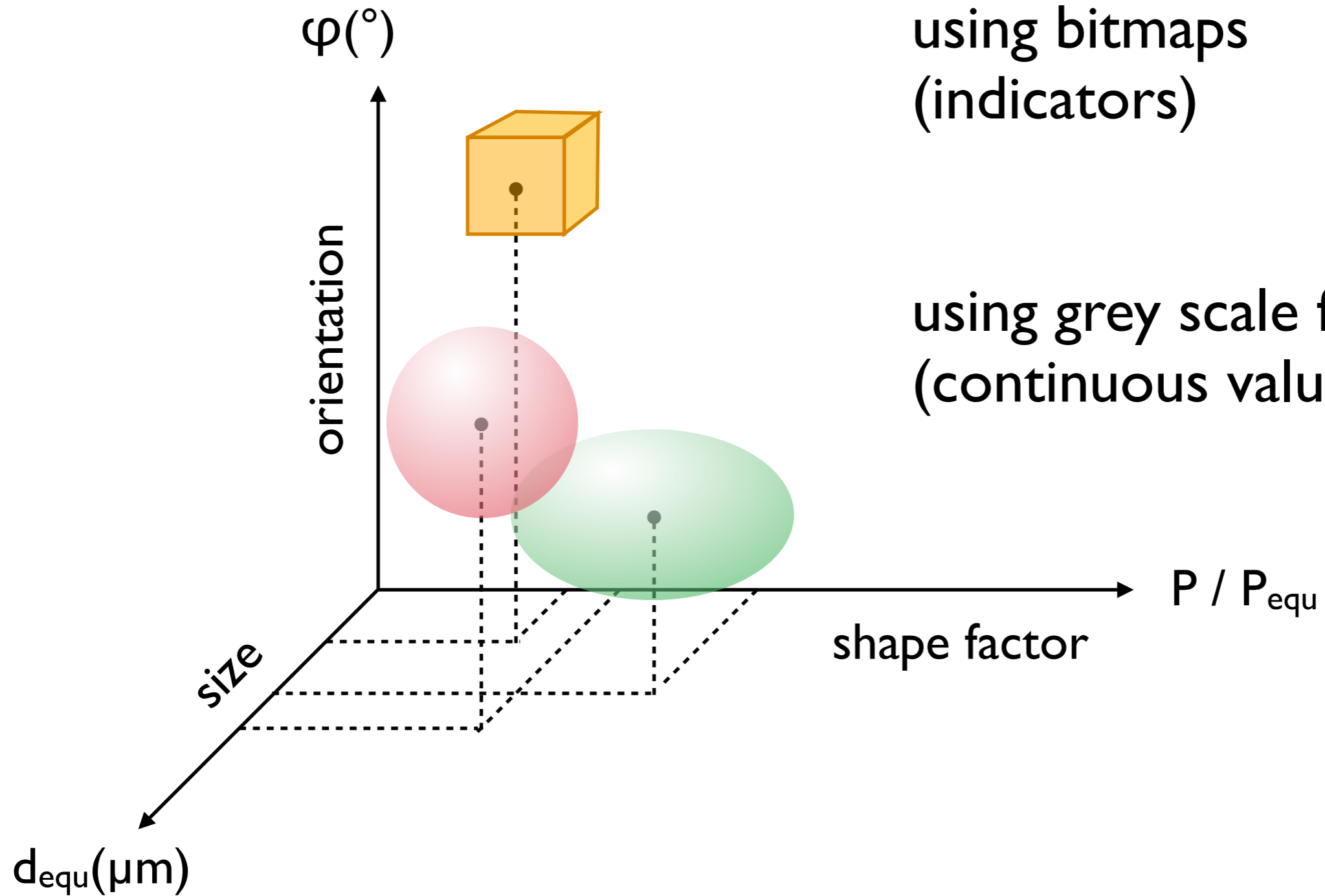


$(15^\circ < \varphi < 45^\circ)$   
 $\cap (1.75 < a/b)$



$(1.5 < \text{SFI} < 2.0) \cap (1.75 < a/b) \cap (15^\circ < \varphi < 45^\circ)$

# feature space



using bitmaps  
(indicators)

using grey scale feature maps  
(continuous values)

# take-home message(s)

- use image analysis (processing) to measure - not to illustrate
- use state-of-the-art image analysis to match state-of-the-art experimentation
- think twice before declaring "the mean grain size"
- use modes of 3D grains - they are most meaningful
- put the numbers back into the picture → map → visualize
- think of images as maps → be quantitative → scale and calibrate  
(you can observe a lot by watching) → (you can understand a lot by measuring)
- think of microstructures as multidimensional → plot data in feature space (= intersect images)

*... and be happy if you do not get a simple answer*



# announcement



## European Geosciences Union General Assembly 2016

Vienna | Austria | 17–22 April 2016

EGU.eu



### TS1 – Brittle Deformation and Fault-related Processes

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### TS2 – Ductile Deformation, Metamorphism and Magmatism

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#### Suggested Session

**Advances in Microstructure and Texture Analysis** 🔍

**[Suggest a new Title]**

Conveners: Renee Heilbronner, Rüdiger Kilian

**[Suggest a Convener and Description Change]**